Electric Potential, Electric Potential Energy and Capacitance

Chapter 18



Part 1

Electric Potential Energy



Physics 111: Potential Energy

Potential energy U is energy that can be associated with the configuration of a system of objects that exert forces on one another. If the configuration of the system changes, then the potential energy of the system can also change

Potential energy can be defined for conservative forces only

5

Examples:

- gravitational potential energy
- spring elastic potential energy

Connection between energy and force - hint

$$\Delta K = \frac{mv^2}{2} - \frac{mv_0^2}{2} \qquad v^2 - v_0^2 = 2a(x - x_0)$$
$$\Delta K = \frac{1}{2}m(v^2 - v_0^2) = ma(x - x_0)$$
$$\boxed{\frac{1}{2}mv^2 - \frac{1}{2}mv_0^2 = F(x - x_0)}$$

Left side – the kinetic energy has been changed Right side – the change is equal to F_x d

 $W = F(x - x_0)$

Similarities between Coulomb's law and Newton's gravitational law

Equations are similar

$$F_g = G \frac{m_1 m_2}{r^2} \qquad F_c = k \frac{q_1 q_2}{r^2}$$

Both forces are conservative ones. <u>Conservative force</u>: Definition 1. A conservative force does zero total work on any closed path Definition 2. The work done by a conservative force in some from an arbitrary point A to an arbitrary point P

going from an arbitrary point A to an arbitrary point B is independent of the path from A to B $$_7$$

Connection between a <u>conservative</u> force and potential energy

The change in potential energy dues to the change in configuration

Calculus based physics

$$\Delta U = -\int F(x)dx$$

Algebra based physics (gravitational and spring forces) $\Delta U = mgh \quad F = mg$

$$\Delta U = -\frac{1}{2}kx^2 \quad F = -kx$$













More terminology	
Electric potential energy (U):	
potential energy	
electrostatic potential energy	
Electric potential (V):	
potential	
potential difference	
voltage (difference)	
electrostatic potential	
	16





Conservation of energy

A consequence of the fact that electric force is conservative is that the total energy of an object is conserved (as long as non-conservative forces like friction can be ignored)

$$\frac{K_a + U_a = K_b + U_b}{\frac{1}{2}mv_a^2 + qV_a = \frac{1}{2}mv_b^2 + qV_b}$$



















One proton

A proton is released from rest in a region of space with non-zero electric field. As the proton moves, does the electric potential energy of the proton increase, decrease or stay the same? Explain. ?



Two protons (more)

Two protons are released from rest when they are D nm apart.

- (a) What is the maximum speed they will reach?(b) What is the maximum acceleration they will
- achieve?
- (c) When does this acceleration occur?
- (d) Will the answers to questions a-c be different if
- we consider two electrons?
- (e) What if we have an electron and a proton?
- 31

U

?

The Electron Volt It is often convenient to work with a unit of energy called the electron volt. One electron volt is defined as the amount of energy an electron (with charge *e*) gains when accelerated through a potential difference of -1 *V*: $1 \text{ eV} = (1.6 \times 10^{-19} \text{ C})\text{V} = 1.6 \times 10^{-19} \text{ J}$













Storing energy as potential energy: stretching a spring lifting a book pulling a bowstring We can also store energy as potential energy in an electric field. Capacitor is a device that is used to do that.









Question

A capacitor ${\cal C}$ "has a charge Q". The actual charges on its plates are:

- A) Q, QB) Q/2, Q/2
- C) Q, -Q
- D) Q/2, -Q/2
- E) Q, 0

?

43

Energy stored in an electric field

Electric potential energy of a charged capacitor



The potential energy of a charged capacitor may be viewed as being stored in the electric field between its plates

44

Capacitor with dielectric Dielectric: insulating material (plastic, paper ...) $C = \kappa C_0$ k is the dielectric constant 1.00054 air paper 3.5 12.0 Silicon Water 80.4 Titania ceramic 130.0 45

	?
Question	
A parallel-plate capacitor is attached to a battery that maintains a constant potential difference V between the plates. While the battery is still connected, a glass slat inserted so as to just fill the space between the plates. The stored energy 1. increases. 2. decreases. 3. remains the same.	ie D is
	46