

## Models of Acids and Bases

-Arrhenius Concept: Acids produce $\mathrm{H}^{+}$in solution, bases produce $\mathrm{OH}^{-}$ion.

- Brønsted-Lowry: Acids are $\mathrm{H}^{+}$donors, bases are proton acceptors.
-Review Chapter 4 - Acids \& Bases, Section 4.8

$$
\begin{aligned}
& \mathrm{HCl}+\mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{Cl}^{-}+\mathrm{H}_{3} \mathrm{O}^{+} \\
& \text {acid base }
\end{aligned}
$$



## Conjugate Acid/Base Pairs


-conjugate base: everything that remains of the acid molecule after a proton is lost.
-conjugate acid: formed when the proton is transferred to the base.


## CONCEPT CHECK 16.1

Chemists in the seventeenth century discovered that the substance that gives red ants their irritating bite is an acid with the formula $\mathrm{HCHO}_{2}$. They called this substance formic acid after the ant, whose Latin name is formica rufus. Formic acid has the following structural formula and molecular model:


Write the acid-base equilibria connecting all components in the aqueous solution. Now list all of the species present.

$\underset{\text { HCOOH }}{\text { formic acid }}+\underset{\text { water }}{\mathrm{H}_{2} \mathrm{O}} \rightleftharpoons \underset{\text { formate ion }}{\mathrm{HCOO}^{-}+} \quad$| $\mathrm{H}_{3} \mathrm{O}^{+}$ |
| :--- |
| hydronium ion |

## Acid Strength

## Strong Acid:

齂 Its equilibrium position lies far to the right. $\left(\mathrm{HNO}_{3}\right)$
Yields a weak conjugate base. $\left(\mathrm{NO}_{3}{ }^{-}\right)$

$$
\mathrm{HNO}_{3}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightarrow \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{NO}_{3}^{-}(\mathrm{aq})
$$

$\mathrm{K}_{\mathrm{a}} \gg 1$ We do not usually consider the reactants in reactions because the are present in very small amounts!

## Acid Strength <br> (continued)

## Weak Acid:

Its equilibrium lies far to the left. $\left(\mathrm{CH}_{3} \mathrm{COOH}\right)$
鱼 Yields a much stronger (it is relatively strong) conjugate base than water. $\left(\mathrm{CH}_{3} \mathrm{COO}^{-}\right)$
$\mathrm{HC}_{2} \mathrm{H}_{3} \mathrm{O}_{2}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2}^{-}(\mathrm{aq})$
$\mathrm{K}_{\mathrm{a}} \ll 1$ Equilibrium favors reactants - but the solution is still acidic - so acetic acid IS an acid!


Weak \& Strong Acids: (a) A strong acid HA is completely ionized in water. (b) A weak acid HB exists mostly as undissociated HB molecules in water. Note that the water molecules are not shown in this figure.


Figure 14.4: Graphic representation of the behavior of acids of different strengths in aqueous solution. (a) A strong acid. (b) A weak acid.


TABLE 14.1 Various Ways to Describe Acid Strength

| Property | Strong Acid | Weak Acid |
| :---: | :---: | :---: |
| $K_{\mathrm{a}}$ value | $K_{\mathrm{a}}$ is large | $K_{\mathrm{a}}$ is small |
| Position of the dissociation (ionization) equilibrium | Far to the right | Far to the left |
| Equilibrium concentration of $\mathrm{H}^{+}$compared with original concentration of HA | $\left[\mathrm{H}^{+}\right] \approx[\mathrm{HA}]_{0}$ | $\left[\mathrm{H}^{+}\right] \ll[\mathrm{HA}]_{0}$ |
| Strength of conjugate base compared with that of water | $\mathrm{A}^{-}$much weaker base than $\mathrm{H}_{2} \mathrm{O}$ | $\mathrm{A}^{-}$much stronger base than $\mathrm{H}_{2} \mathrm{O}$ |

## Bases

-"Strong" and "weak" are used in the same sense for bases as for acids.
-strong $=$ complete dissociation (hydroxide ion supplied to solution)

$$
\cdot \mathrm{NaOH}(s) \rightarrow \mathrm{Na}^{+}(a q)+\mathrm{OH}^{-}(a q)
$$

$$
\mathrm{K}_{\mathrm{b}} \gg 1
$$

## Bases

(continued)
-weak $=$ very little dissociation (or reaction with water)

$$
\begin{gathered}
\cdot \mathrm{CH}_{3} \mathrm{NH}_{2}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{CH}_{3} \mathrm{NH}_{3}^{+}(a q)+\mathrm{OH}^{-}(a q) \\
\mathrm{K}_{\mathrm{b}} \ll 1
\end{gathered}
$$

## TABLE 14.3 Values of $\boldsymbol{K}_{\mathrm{b}}$ for Some Common Weak Bases

| Name | Formula | Conjugate <br> Acid | $K_{\mathrm{b}}$ |
| :--- | :--- | :--- | ---: |
| Ammonia | $\mathrm{NH}_{3}$ | $\mathrm{NH}_{4}{ }^{+}$ | $1.8 \times 10^{-5}$ |
| Methylamine | $\mathrm{CH}_{3} \mathrm{NH}_{2}$ | $\mathrm{CH}_{3} \mathrm{NH}_{3}{ }^{+}$ | $4.38 \times 10^{-4}$ |
| Ethylamine | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{NH}_{2}$ | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{NH}_{3}{ }^{+}$ | $5.6 \times 10^{-4}$ |
| Aniline | $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{2}$ | $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{3}{ }^{+}$ | $3.8 \times 10^{-10}$ |
| Pyridine | $\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}$ | $\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{NH}^{+}$ | $1.7 \times 10^{-9}$ |




## Figure 14.7: Two water molecules react to form $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{OH}^{-}$.



$$
\begin{gathered}
2 \mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq}) \\
{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{OH}^{-}\right]=\mathrm{K}_{\mathrm{w}}=1.01 \times 10^{-14}}
\end{gathered}
$$

CONCEPT CHECK 16.2
Formic acid, $\mathrm{HCHO}_{2}$, is a stronger acid than acetic acid, $\mathrm{HC}_{2} \mathrm{H}_{3} \mathrm{O}_{2}$. Which is the stronger base, formate ion, $\mathrm{CHO}_{2}{ }^{-}$, or acetate ion, $\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2}{ }^{-}$?

Acetic Acid: $\mathrm{K}_{\mathrm{a}}=1.8 \times 10^{-5}$
Formic Acid: $\mathrm{K}_{\mathrm{a}}=1.8 \times 10^{-4}$
Acetate ion: $\mathrm{K}_{\mathrm{b}}=5 \times 10^{-10}$
Formate ion: $\mathrm{K}_{\mathrm{b}}=5 \times 10^{-11}$

Acetate ion!

## Solutions of Strong Acid or Base

- In a solution of a strong acid you can normally ignore the self-ionization of water as a source of $\mathrm{H}^{+}(\mathrm{aq})$.
- The $\mathrm{H}^{+}(\mathrm{aq})$ concentration is usually determined by the strong acid concentration.
- However, the self-ionization still exists and is responsible for a small concentration of $\mathrm{OH}^{-}$
ion.

$$
\begin{aligned}
& \mathrm{H}^{+}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightarrow \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq}) \mathrm{K}_{\mathrm{a}} \gg 1 \\
& 2 \mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq}) \mathrm{K}_{\mathrm{a}}=1.0 \times 10^{-14}
\end{aligned}
$$

## Self-ionization of Water

- These ions are produced in equal numbers in pure water, so if we let $x=\left[\mathrm{H}^{+}\right]=\left[\mathrm{OH}^{-}\right]$

$$
\begin{aligned}
& 1.0 \times 10^{-14}=(x)(x) \quad \text { at } 25^{0} \mathrm{C} \\
& x=\sqrt{1.0 \times 10^{-14}}=1.0 \times 10^{-7}
\end{aligned}
$$

- Thus, the concentrations of $\mathrm{H}^{+}$and $\mathrm{OH}^{-}$in pure water are both $1.0 \times 10^{-7} \mathrm{M}$.
- If you add acid or base to water they are no longer equal but the $\mathrm{K}_{\mathrm{w}}$ expression still holds.


## Solutions of Strong Acid or Base

- As an example, calculate the concentration of $\mathrm{OH}^{-}$ ion in 0.10 M HCl .

Because you started with 0.10 M HCl (a strong acid) the reaction will produce $0.10 \mathrm{M} \mathrm{H}^{+}(\mathrm{aq})$.

$$
\mathrm{HCl}(\mathrm{aq}) \rightarrow \mathrm{H}^{+}(\mathrm{aq})+\mathrm{Cl}^{-}(\mathrm{aq})
$$

- Substituting $\left[\mathrm{H}^{+}\right]=0.10$ into the ion-product expression, we get:

$$
1.0 \times 10^{-14}=(0.10)\left[\mathrm{OH}^{-}\right]
$$

## Solutions of Strong Acid or

 Base- As an example, calculate the concentration of $\mathrm{OH}^{-}$ ion in 0.10 M HCl .

Because you started with 0.10 M HCl (a strong acid) the reaction will produce $0.10 \mathrm{M} \mathrm{H}^{+}(\mathrm{aq})$.

$$
\mathrm{HCl}(\mathrm{aq}) \rightarrow \mathrm{H}^{+}(\mathrm{aq})+\mathrm{Cl}^{-}(\mathrm{aq})
$$

- Substituting $\left[\mathrm{H}^{+}\right]=0.10$ into the ion-product expression, we get:

$$
\left[\mathrm{OH}^{-}\right]=\frac{1.0 \times 10^{-14}}{0.10}=1.0 \times 10^{-13} \mathrm{M}
$$

## Solutions of Strong Acid or Base

- Similarly, in a solution of a strong base you can normally ignore the self-ionization of water as a source of $\mathrm{OH}^{-}(\mathrm{aq})$.
- The $\mathrm{OH}^{-}(\mathrm{aq})$ concentration is usually determined by the strong base concentration.
- However, the self-ionization still exists and is responsible for a small concentration of $\mathrm{H}^{+}$ion.


## Solutions of Strong Acid or

## Base

- As an example, calculate the concentration of $\mathrm{H}^{+}$
ion in 0.010 M NaOH . Because you started with 0.010 M NaOH (a strong base) the reaction will produce $0.010 \mathrm{M} \mathrm{OH}^{-}(\mathrm{aq})$.
$\mathrm{NaOH}(\mathrm{s}) \xrightarrow{\mathrm{H}_{2} \mathrm{O}} \mathrm{Na}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})$
- Substituting $\left[\mathrm{OH}^{-}\right]=0.010$ into the ion-product expression, we get:

$$
1.0 \times 10^{-14}=\left[\mathrm{H}^{+}\right](0.010)
$$

## Solutions of Strong Acid or

## Base

- At $25^{\circ} \mathrm{C}$, you observe the following conditions.
- In an acidic solution, $\left[\mathrm{H}^{+}\right]>1.0 \times 10^{-7} \mathrm{M}$.
- In a neutral solution, $\left[\mathrm{H}^{+}\right]=1.0 \times 10^{-7} \mathrm{M}$.
- In a basic solution, $\quad\left[\mathrm{H}^{+}\right]<1.0 \times 10^{-7} \mathrm{M}$.


## Solutions of Strong Acid or Base

- As an example, calculate the concentration of $\mathrm{H}^{+}$ ion in 0.010 M NaOH . Because you started with 0.010 M NaOH (a strong base) the reaction will produce $0.010 \mathrm{M} \mathrm{OH}^{-}(\mathrm{aq})$.
$\mathrm{NaOH}(\mathrm{s}) \xrightarrow{\mathrm{H}_{2} \mathrm{O}} \mathrm{Na}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})$
- Substituting $\left[\mathrm{OH}^{-}\right]=0.010$ into the ion-product expression, we get:

$$
\left[H^{+}\right]=\frac{1.0 \times 10^{-14}}{0.010}=1.0 \times 10^{-12} \mathrm{M}
$$

## The pH Scale

- $\mathrm{pH} \approx-\log \left[\mathrm{H}^{+}\right]$
- pH in water ranges from 0 to 14 .
- $K_{\mathrm{w}}=1.00 \times 10^{-14}=\left[\mathrm{H}^{+}\right]\left[\mathrm{OH}^{-}\right]$
- $\mathrm{p} K_{\mathrm{w}}=14.00=\mathrm{pH}+\mathrm{pOH}$
- As pH rises, pOH falls (sum = 14.00).


## The $\mathbf{p H}$ of a Solution

- For a solution in which the hydrogen-ion concentration is $1.0 \times 10^{-3}$, the pH is:

$$
p H=-\log \left(1.0 \times 10^{-3}\right)=3.00
$$

- Note that the number of decimal places in the pH equals the number of significant figures in the hydrogen-ion concentration.


## The $\mathbf{p H}$ of a Solution

- In a neutral solution, whose hydrogen-ion concentration is $1.0 \times 10^{-7}$, the $\mathrm{pH}=7.00$.
- For acidic solutions, the hydrogen-ion concentration is greater than $1.0 \times 10^{-7}$, so the pH is less than 7.00.
- Similarly, a basic solution has a pH greater than 7.00.
- Figure 16.6 shows a diagram of the pH scale and the pH values of some common solutions.



## A Problem to Consider

- The pH of human arterial blood is 7.40 . What is the hydrogen-ion concentration?

$$
\left[\mathbf{H}^{+}\right]=\operatorname{anti} \log (-\mathbf{p H})
$$

$$
\left[\mathrm{H}^{+}\right]=\operatorname{anti} \log (-7.40)
$$

$$
\left[\mathrm{H}^{+}\right]=10^{-7.40}=4.0 \times 10^{-8} \mathrm{M}
$$

## A Problem to Consider

- A sample of orange juice has a hydrogen-ion concentration of $2.9 \times 10^{-4} \mathrm{M}$. What is the pH ?

$$
\begin{aligned}
& \mathrm{pH}=-\log \left[\mathrm{H}^{+}\right] \\
& \mathrm{pH}=-\log \left(2.9 \times 10^{-4}\right) \\
& \mathrm{pH}=3.54
\end{aligned}
$$

## The pH of a Solution

- A measurement of the hydroxide ion concentration, similar to pH , is the pOH .
- The pOH of a solution is defined as the negative logarithm of the molar hydroxide-ion concentration.

$$
\mathrm{pOH}=-\log \left[\mathrm{OH}^{-}\right]
$$

## The pH of a Solution

- A measurement of the hydroxide ion concentration, similar to pH , is the pOH .
- Then because $\mathrm{K}_{\mathrm{w}}=\left[\mathrm{H}^{+}\right][\mathrm{OH}]=1.0 \times 10^{-14}$ at $25^{\circ} \mathrm{C}$, you can show that

$$
\mathrm{pH}+\mathrm{pOH}=14.00
$$

## A Problem to Consider

- An ammonia solution has a hydroxide-ion concentration of $1.9 \times 10^{-3} \mathrm{M}$. What is the pH of the solution?
You first calculate the pOH :
$\mathrm{pOH}=-\log \left(1.9 \times 10^{-3}\right)=2.72$
Then the pH is:

$$
\mathrm{pH}=14.00-2.72=11.28
$$

## The pH of a Solution

- The pH of a solution can accurately be measured using a pH meter
- Although less precise, acid-base indicators are often used to measure pH because they usually change color within a narrow pH range.
- Figure 16.8 shows the color changes of various acid-base indicators.

Figure 14.9: pH meters are used to measure acidity.


Figure 16.8: Color changes of some acidbased indicators.


Percent Dissociation (Degree of Ionization)
$\%$ dissociation $=\frac{\operatorname{amount} \operatorname{dissociated}(M)}{\text { initial concentration }(M)} \times 100 \%$

Weak acids and bases have low values for
$\%$ dissociation - their degree of ionization is small.

## A Problem To Consider

- Nicotinic acid is a weak monoprotic acid with the formula $\mathrm{HC}_{6} \mathrm{H}_{4} \mathrm{NO}_{2}$. A 0.012 M solution of nicotinic acid has a pH of 3.39 at $25^{\circ} \mathrm{C}$.
$\left[\mathrm{H}^{+}\right]=10^{-3.39}=0.00041$
- To obtain the degree of dissociation:

Degree of dissociation $=\frac{0.00041}{0.012}=0.034$

- The percent ionization is obtained by multiplying by 100 , which gives $3.4 \%$.


## A Problem To Consider

- Nicotinic acid is a weak monoprotic acid with the formula $\mathrm{HC}_{6} \mathrm{H}_{4} \mathrm{NO}_{2}$. A 0.012 M solution of nicotinic acid has a pH of 3.39 at $25^{\circ} \mathrm{C}$. Calculate the acidionization constant for this acid at $25^{\circ} \mathrm{C}$.
- It is important to realize that the solution was made 0.012 M in nicotinic acid, however, some molecules ionize making the equilibrium concentration of nicotinic acid less than 0.012 M .
- We will abbreviate the formula for nicotinic acid as HNic.


## A Problem To Consider

- Nicotinic acid is a weak monoprotic acid with the formula $\mathrm{HC}_{6} \mathrm{H}_{4} \mathrm{NO}_{2}$. A 0.012 M solution of nicotinic acid has a pH of 3.39 at $25^{\circ} \mathrm{C}$. Calculate the acidionization constant for this acid at $25^{\circ} \mathrm{C}$.
- Let x be the moles per liter of product formed.

$$
\mathrm{HNic}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftarrows \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{Nic}^{-}(\mathrm{aq})
$$

| Initial | 0.012 |
| :---: | :---: |
| Change | -x |
| Equilibrium | $0.012-\mathrm{x}$ |


| 0 | 0 |
| :---: | :---: |
| +x | +x |
| x | x |

## A Problem To Consider

- Nicotinic acid is a weak monoprotic acid with the formula $\mathrm{HC}_{6} \mathrm{H}_{4} \mathrm{NO}_{2}$. A 0.012 M solution of nicotinic acid has a pH of 3.39 at $25^{\circ} \mathrm{C}$. Calculate the acidionization constant for this acid at $25^{\circ} \mathrm{C}$.
- The equilibrium-constant expression is:

$$
\mathrm{K}_{\mathrm{a}}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{Nic}^{-}\right]}{[\mathrm{HNic}]}
$$

## A Problem To Consider

- Nicotinic acid is a weak monoprotic acid with the formula $\mathrm{HC}_{6} \mathrm{H}_{4} \mathrm{NO}_{2}$. A 0.012 M solution of nicotinic acid has a pH of 3.39 at $25^{\circ} \mathrm{C}$. Calculate the acidionization constant for this acid at $25^{\circ} \mathrm{C}$.
- We can obtain the value of x from the given pH .

$$
\begin{aligned}
& \mathrm{x}=\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\operatorname{anti} \log (-\mathrm{pH}) \\
& \mathrm{x}=\operatorname{antilog}(-3.39) \\
& \mathrm{x}=4.1 \times 10^{-4}=0.00041
\end{aligned}
$$

## A Problem To Consider

- Nicotinic acid is a weak monoprotic acid with the formula $\mathrm{HC}_{6} \mathrm{H}_{4} \mathrm{NO}_{2}$. A 0.012 M solution of nicotinic acid has a pH of 3.39 at $25^{\circ} \mathrm{C}$. Calculate the acidionization constant for this acid at $25^{\circ} \mathrm{C}$.
- Substituting the expressions for the equilibrium concentrations, we get

$$
\mathbf{K}_{\mathrm{a}}=\frac{\mathbf{x}^{2}}{(0.012-\mathbf{x})}
$$

## A Problem To Consider

- Nicotinic acid is a weak monoprotic acid with the formula $\mathrm{HC}_{6} \mathrm{H}_{4} \mathrm{NO}_{2}$. A 0.012 M solution of nicotinic acid has a pH of 3.39 at $25^{\circ} \mathrm{C}$. Calculate the acidionization constant for this acid at $25^{\circ} \mathrm{C}$.
- Substitute this value of $x$ in our equilibrium expression.
- Note first, however, that
$\mathbf{( 0 . 0 1 2}-\mathbf{x})=\mathbf{( 0 . 0 1 2}-\mathbf{0 . 0 0 0 4 1})=\mathbf{0 . 0 1 1 5 9} \cong 0.012$
the concentration of unionized acid remains virtually unchanged.


## Solving Weak Acid Equilibrium Problems

List major species in solution.
Choose species that can produce $\mathrm{H}^{+}$and write reactions.

Based on K values, decide on dominant equilibrium.
(1) Write equilibrium expression for dominant equilibrium.
(e) List initial concentrations in dominant equilibrium.

## Calculations With $\mathbf{K}_{\mathrm{a}}$

- If you know the value of $K_{a}$, you can calculate the equilibrium concentrations of species $\mathrm{HA}, \mathrm{A}^{-}$, and $\mathrm{H}_{3} \mathrm{O}^{+}$for solutions of different molarities.


## A Problem To Consider

- Nicotinic acid is a weak monoprotic acid with the formula $\mathrm{HC}_{6} \mathrm{H}_{4} \mathrm{NO}_{2}$. A 0.012 M solution of nicotinic acid has a pH of 3.39 at $25^{\circ} \mathrm{C}$. Calculate the acidionization constant for this acid at $25^{\circ} \mathrm{C}$.
- Substitute this value of $x$ in our equilibrium expression.

$$
K_{a}=\frac{x^{2}}{(0.012-x)} \cong \frac{(0.00041)^{2}}{(0.012)}=1.4 \times 10^{-5}
$$

## Solving Weak Acid Equilibrium Problems (continued)

(1) Define change at equilibrium (as " $x$ ").
(1) Write equilibrium concentrations in terms of $x$.

國 Substitute equilibrium concentrations into equilibrium expression.
-1 Solve for $x$ the "easy way."
(1) Verify assumptions using $5 \%$ rule.
(1) Calculate $\left[\mathrm{H}^{+}\right]$and pH .

## Calculations With $\mathbf{K}_{\mathbf{a}}$

- Note that in our previous example, the degree of dissociation was so small that " $x$ " was negligible compared to the concentration of nicotinic acid.
- It is the small value of the degree of ionization that allowed us to ignore the subtracted $x$ in the denominator of our equilibrium expression.
- The degree of ionization of a weak acid depends on both the $\mathrm{K}_{\mathrm{a}}$ and the concentration of the acid solution.


## Calculations With $\mathbf{K}_{\mathrm{a}}$

- How do you know when you can use this simplifying assumption?
- It can be shown that if the acid concentration, $C_{a}$, divided by the $K_{a}$ exceeds 100 , that is,

$$
\text { if } \mathrm{C}_{\mathrm{a}} \mathrm{~K}_{\mathrm{a}}>100
$$

then this simplifying assumption of ignoring the subtracted $\mathbf{x}$ gives an acceptable error of less than $5 \%$.

## Calculations With $\mathbf{K}_{\mathrm{a}}$

- How do you know when you can use this simplifying assumption?
- If the simplifying assumption is not valid, you can solve the equilibrium equation exactly by using the quadratic equation.
- The next example illustrates this with a solution of aspirin (acetylsalicylic acid), $\mathrm{HC}_{9} \mathrm{H}_{7} \mathrm{O}_{4}$, a common headache remedy.


## A Problem To Consider

- What is the pH at $25^{\circ} \mathrm{C}$ of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\mathrm{HC}_{9} \mathrm{H}_{7} \mathrm{O}_{4}$, in 0.500 L of water? The acid is monoprotic and $\mathrm{K}_{\mathrm{a}}=3.3 \times 10^{-4}$ at $25^{\circ} \mathrm{C}$.
- The molar mass of $\mathrm{HC}_{9} \mathrm{H}_{7} \mathrm{O}_{4}$ is 180.2 g .

From this we find that the sample contained 0.00180 mol of the acid.

## A Problem To Consider

- What is the pH at $25^{\circ} \mathrm{C}$ of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\mathrm{HC}_{9} \mathrm{H}_{7} \mathrm{O}_{4}$, in 0.500 L of water? The acid is monoprotic and $\mathrm{K}_{\mathrm{a}}=3.3 \times 10^{-4}$ at $25^{\circ} \mathrm{C}$.
- The molar mass of $\mathrm{HC}_{9} \mathrm{H}_{7} \mathrm{O}_{4}$ is 180.2 g .

Hence, the concentration of the acetylsalicylic acid is $0.00180 \mathrm{~mol} / 0.500 \mathrm{~L}=0.0036 \mathrm{M}$ (Retain two significant figures, the same number of significant figures in $\mathrm{K}_{\mathrm{a}}$ ).

## A Problem To Consider

- What is the pH at $25^{\circ} \mathrm{C}$ of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\mathrm{HC}_{9} \mathrm{H}_{7} \mathrm{O}_{4}$, in 0.500 L of water? The acid is monoprotic and $\mathrm{K}_{\mathrm{a}}=3.3 \times 10^{-4}$ at $25^{\circ} \mathrm{C}$.
- Note that

$$
\mathrm{C}_{\mathrm{a}} / \mathrm{K}_{\mathrm{a}}=0.0036 / 3.3 \times 10^{-4}=11
$$

which is less than 100 , so we must solve the equilibrium equation exactly.

## A Problem To Consider

- What is the pH at $25^{\circ} \mathrm{C}$ of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\mathrm{HC}_{9} \mathrm{H}_{7} \mathrm{O}_{4}$, in 0.500 L of water? The acid is monoprotic and $\mathrm{K}_{\mathrm{a}}=3.3 \times 10^{-4}$ at $25^{\circ} \mathrm{C}$.
- We will abbreviate the formula for acetylsalicylic acid as HAcs and let $\mathbf{x}$ be the amount of $\mathrm{H}_{3} \mathrm{O}^{+}$formed per liter.
- The amount of acetylsalicylate ion is also $\mathbf{x} \mathrm{mol}$; the amount of nonionized acetylsalicylic acid is (0.0036-x) mol.


## A Problem To Consider

- What is the pH at $25^{\circ} \mathrm{C}$ of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\mathrm{HC}_{9} \mathrm{H}_{7} \mathrm{O}_{4}$, in 0.500 L of water? The acid is monoprotic and $\mathrm{K}_{\mathrm{a}}=3.3 \times 10^{-4}$ at $25^{\circ} \mathrm{C}$.
- These data are summarized below.
$\mathrm{HAcs}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftarrows \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\operatorname{Acs}^{-}(\mathrm{aq})$

| Initial | 0.0036 |
| :---: | :---: |
| Change | -x |
| Equilibrium | $0.0036-\mathrm{x}$ |


| 0 | 0 |
| :---: | :---: |
| +x | +x |
| x | x |

## A Problem To Consider

- What is the pH at $25^{\circ} \mathrm{C}$ of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\mathrm{HC}_{9} \mathrm{H}_{7} \mathrm{O}_{4}$, in 0.500 L of water? The acid is monoprotic and $\mathrm{K}_{\mathrm{a}}=3.3 \times 10^{-4}$ at $25^{\circ} \mathrm{C}$.
- If we substitute the equilibrium concentrations and the $\mathrm{K}_{\mathrm{a}}$ into the equilibrium constant expression, we get

$$
\frac{x^{2}}{(0.0036-x)}=3.3 \times 10^{-4}
$$

## A Problem To Consider

- What is the pH at $25^{\circ} \mathrm{C}$ of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\mathrm{HC}_{9} \mathrm{H}_{7} \mathrm{O}_{4}$, in 0.500 L of water? The acid is monoprotic and $\mathrm{K}_{\mathrm{a}}=3.3 \times 10^{-4}$ at $25^{\circ} \mathrm{C}$.
- The equilibrium constant expression is

$$
\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{Acs}^{-}\right]}{[\mathrm{HAcs}]}=\mathrm{K}_{\mathrm{a}}
$$

## A Problem To Consider

- What is the pH at $25^{\circ} \mathrm{C}$ of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\mathrm{HC}_{9} \mathrm{H}_{7} \mathrm{O}_{4}$, in 0.500 L of water? The acid is monoprotic and $\mathrm{K}_{\mathrm{a}}=3.3 \times 10^{-4}$ at $25^{\circ} \mathrm{C}$.
- You can solve this equation exactly by using the quadratic formula.
- Rearranging the preceding equation to put it in the form $\mathrm{ax}^{2}+\mathrm{bx}+\mathrm{c}=0$, we get

$$
x^{2}+\left(3.3 \times 10^{-4}\right) x-\left(1.2 \times 10^{-6}\right)=0
$$

## A Problem To Consider

- What is the pH at $25^{\circ} \mathrm{C}$ of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\mathrm{HC}_{9} \mathrm{H}_{7} \mathrm{O}_{4}$, in 0.500 L of water? The acid is monoprotic and $\mathrm{K}_{\mathrm{a}}=3.3 \times 10^{-4}$ at $25^{\circ} \mathrm{C}$.
- Now substitute into the quadratic formula.

$$
x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}
$$

## A Problem To Consider

- What is the pH at $25^{\circ} \mathrm{C}$ of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\mathrm{HC}_{9} \mathrm{H}_{7} \mathrm{O}_{4}$, in 0.500 L of water? The acid is monoprotic and $\mathrm{K}_{\mathrm{a}}=3.3 \times 10^{-4}$ at $25^{\circ} \mathrm{C}$.
- Now substitute into the quadratic formula.

$$
x=\frac{-\left(3.3 \times 10^{-4}\right) \pm \sqrt{\left(3.3 \times 10^{-4}\right)^{2}-4\left(1.2 \times 10^{-6}\right)}}{2}
$$

- The lower sign in $\pm$ gives a negative root which we can ignore


## A Problem To Consider

- What is the pH at $25^{\circ} \mathrm{C}$ of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\mathrm{HC}_{9} \mathrm{H}_{7} \mathrm{O}_{4}$, in 0.500 L of water? The acid is monoprotic and $\mathrm{K}_{\mathrm{a}}=3.3 \times 10^{-4}$ at $25^{\circ} \mathrm{C}$.
- Taking the upper sign, we get

$$
\mathrm{x}=\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=9.4 \times 10^{-4}
$$

- Now we can calculate the pH .

$$
\mathrm{pH}=-\log \left(9.4 \times 10^{-4}\right)=3.03
$$

## A Problem To Consider

- What is the pH of a 0.20 M solution of pyridine, $\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}$, in aqueous solution? The $\mathrm{K}_{\mathrm{b}}$ for pyridine is $1.4 \times 10^{-9}$.
- As before, we will follow the three steps in solving an equilibrium.

1. Write the equation and make a table of concentrations.
2. Set up the equilibrium constant expression.
3. Solve for $x=\left[\mathrm{OH}^{-}\right]$.

## A Problem To Consider (Weak Base)

- What is the pH of a 0.20 M solution of pyridine, $\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}$, in aqueous solution? The $\mathrm{K}_{\mathrm{b}}$ for pyridine is $1.4 \times 10^{-9}$.
- Pyridine ionizes by picking up a proton from water (as ammonia does).
$\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \longleftrightarrow \mathrm{C}_{5} \mathrm{H}_{5} \mathrm{NH}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})$

| Initial | 0.20 |
| :---: | :---: |
| Change | -x |
| Equilibrium | $0.20-\mathrm{x}$ |


| 0 | 0 |
| :---: | :---: |
| +x | +x |
| x | x |

## A Problem To Consider

- What is the pH of a 0.20 M solution of pyridine, $\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}$, in aqueous solution? The $\mathrm{K}_{\mathrm{b}}$ for pyridine is $1.4 \times 10^{-9}$.
- Note that
$C_{a} / K_{a}=0.20 / 1.4 \times 10^{-9}=1.4 \times 10^{8}$
which is much greater than 100 , so we may use the simplifying assumption that $(0.20-\mathrm{x}) \cong(0.20)$.


## A Problem To Consider

- What is the pH of a 0.20 M solution of pyridine, $\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}$, in aqueous solution? The $\mathrm{K}_{\mathrm{b}}$ for pyridine is $1.4 \times 10^{-9}$.
- The equilibrium expression is

$$
\frac{\left[\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{NH}^{+}\right]\left[\mathrm{OH}^{-}\right]}{\left[\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}\right]}=\mathrm{K}_{\mathrm{b}}
$$

## A Problem To Consider

- What is the pH of a 0.20 M solution of pyridine, $\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}$, in aqueous solution? The $\mathrm{K}_{\mathrm{b}}$ for pyridine is $1.4 \times 10^{-9}$.
- If we substitute the equilibrium concentrations and the $\mathrm{K}_{\mathrm{b}}$ into the equilibrium constant expression, we get

$$
\frac{x^{2}}{(0.20-x)}=1.4 \times 10^{-9}
$$

## A Problem To Consider

- What is the pH of a 0.20 M solution of pyridine, $\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}$, in aqueous solution? The $\mathrm{K}_{\mathrm{b}}$ for pyridine is $1.4 \times 10^{-9}$.
- Using our simplifying assumption that the x in the denominator is negligible, we get

$$
\frac{x^{2}}{(0.20)} \cong 1.4 \times 10^{-9}
$$

## A Problem To Consider

- What is the pH of a 0.20 M solution of pyridine, $\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}$, in aqueous solution? The $\mathrm{K}_{\mathrm{b}}$ for pyridine is $1.4 \times 10^{-9}$.
- Solving for x we get

$$
\begin{gathered}
\mathrm{x}^{2} \cong(0.20) \times\left(1.4 \times 10^{-9}\right) \\
\mathrm{x}=\left[\mathrm{OH}^{-}\right] \cong \sqrt{(0.20) \times\left(1.4 \times 10^{-9}\right)}=1.7 \times 10^{-5}
\end{gathered}
$$

## A Problem To Consider

- What is the pH of a 0.20 M solution of pyridine, $\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}$, in aqueous solution? The $\mathrm{K}_{\mathrm{b}}$ for pyridine is $1.4 \times 10^{-9}$.
- Solving for pOH
$\mathrm{pOH}=-\log [\mathrm{OH}-]=-\log \left(1.7 \times 10^{-5}\right)=4.8$
- Since $\mathrm{pH}+\mathrm{pOH}=14.00$
$\mathrm{pH}=14.00-\mathrm{pOH}=14.00-4.8=9.2$


## Polyprotic Acids

- Some acids have two or more protons (hydrogen ions) to donate in aqueous solution. These are referred to as polyprotic acids.
- Sulfuric acid, for example, can lose two protons in aqueous solution.
$\mathrm{H}_{2} \mathrm{SO}_{4}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightarrow \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{HSO}_{4}^{-}(\mathrm{aq})$
$\mathrm{HSO}_{4}{ }^{-}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftarrows \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{SO}_{4}{ }^{2-}(\mathrm{aq})$
- The first proton is lost completely followed by a weak ionization of the hydrogen sulfate ion, $\mathrm{HSO}_{4}{ }^{-}$.


## Polyprotic Acids

- . . . can furnish more than one proton $\left(\mathrm{H}^{+}\right)$ to the solution.

$$
\begin{aligned}
& \mathrm{H}_{2} \mathrm{CO}_{3} \leftrightarrow \mathrm{H}^{+}+\mathrm{HCO}_{3}^{-} \quad\left(K_{\mathrm{a}_{1}}\right) \\
& \mathrm{HCO}_{3}^{-} \leftrightarrow \mathrm{H}^{+}+\mathrm{CO}_{3}^{2-} \quad\left(K_{\mathrm{a}_{2}}\right)
\end{aligned}
$$

## Polyprotic Acids

- Some acids have two or more protons (hydrogen ions) to donate in aqueous solution. These are referred to as polyprotic acids.
- For a weak diprotic acid like carbonic acid, $\mathrm{H}_{2} \mathrm{CO}_{3}$, two simultaneous equilibria must be considered.

$$
\mathrm{H}_{2} \mathrm{CO}_{3}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftarrows \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{HCO}_{3}^{-}(\mathrm{aq})
$$

$\mathrm{HCO}_{3}{ }^{-}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftarrows \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{CO}_{3}{ }^{2-}(\mathrm{aq})$

## Polyprotic Acids

- Some acids have two or more protons (hydrogen ions) to donate in aqueous solution. These are referred to as polyprotic acids.
- Each equilibrium has an associated acidionization constant.

For the loss of the first proton

$$
\mathrm{K}_{\mathrm{a} 1}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{HCO}_{3}^{-}\right]}{\left[\mathrm{H}_{2} \mathrm{CO}_{3}\right]}=4.3 \times 10^{-7}
$$

## Polyprotic Acids

- Some acids have two or more protons (hydrogen ions) to donate in aqueous solution. These are referred to as polyprotic acids.
- Each equilibrium has an associated acidionization constant.

For the loss of the second proton

$$
\mathrm{K}_{\mathrm{a} 2}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{CO}_{3}{ }^{2-}\right]}{\left[\mathrm{HCO}_{3}{ }^{-}\right]}=4.8 \times 10^{-11}
$$

## Polyprotic Acids

- Some acids have two or more protons (hydrogen ions) to donate in aqueous solution. These are referred to as polyprotic acids.
- The second ionization constant, $\mathrm{K}_{\mathrm{a} 2}$, for a polyprotic acid is always smaller than the first ionization constant, $\mathrm{K}_{\mathrm{a} 1}$.
- In the case of a triprotic acid, such as $\mathrm{H}_{3} \mathrm{PO}_{4}$, the third ionization constant, $\mathrm{K}_{\mathrm{a} 3}$, is smaller than the second one, $\mathrm{K}_{\mathrm{a} 2}$.


## Bronsted-Lowry Concept of Acids and Bases

- Some species can act as an acid or a base.
- An amphoteric species is a species that can act either as an acid or a base (it can gain or lose a proton).
- For example, $\mathrm{HCO}_{3}{ }^{-}$acts as a proton donor (an acid) in the presence of $\mathrm{OH}^{-}$
$\mathrm{HCO}_{3}^{-}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq}) \rightarrow \mathrm{CO}_{3}^{-2}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l})$


## Bronsted-Lowry Concept of Acids and Bases

- Some species can act as an acid or a base.
- An amphoteric species is a species that can act either as an acid or a base (it can gain or lose a proton).
Alternatively, $\mathrm{HCO}_{3}$ can act as a proton acceptor (a base) in the presence of HF .
$\mathrm{HCO}_{3}{ }^{-}(\mathrm{aq})+\mathrm{HF}(\mathrm{aq}) \rightarrow \mathrm{H}_{2} \mathrm{CO}_{3}(\mathrm{aq})+\mathrm{F}^{-}(\mathrm{aq})$


## Brønsted-Lowry Concept of Acids and Bases

- The amphoteric characteristic of water is important in the acid-base properties of aqueous solutions.
- Water can also react as a base with the acid HF.

$$
\mathrm{HF}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightarrow \mathrm{F}^{-}(\mathrm{aq})+\mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})
$$



## Acid-Base Properties of a Salt Solution

- One of the successes of the Brønsted-Lowry concept of acids and bases was in pointing out that some ions can act as acids or bases.
- Consider a solution of sodium cyanide, NaCN .

$$
\mathrm{NaCN}(\mathrm{~s}) \xrightarrow{\mathrm{H}_{2} \mathrm{O}} \mathrm{Na}^{+}(\mathrm{aq})+\mathrm{CN}^{-}(\mathrm{aq})
$$

- A 0.1 M solution has a pH of 11.1 and is therefore fairly basic.


## Bronsted-Lowry Concept of Acids and Bases

- The amphoteric characteristic of water is important in the acid-base properties of aqueous solutions.
- Water reacts as an acid with the base $\mathrm{NH}_{3}$.



## Acid-Base Properties of a Salt Solution

- One of the successes of the Brønsted-Lowry concept of acids and bases was in pointing out that some ions can act as acids or bases.
- Sodium ion, $\mathrm{Na}^{+}$, is unreactive with water, but the cyanide ion, $\mathrm{CN}^{-}$, reacts to produce HCN and $\mathrm{OH}^{-}$.
$\mathrm{CN}^{-}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftarrows \mathrm{HCN}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})$


## Acid-Base Properties of a Salt Solution

- The hydrolysis of an ion is the reaction of an ion with water to produce the conjugate acid and hydroxide ion or the conjugate base and hydronium ion.
- The $\mathrm{NH}_{4}{ }^{+}$ion hydrolyzes to the conjugate base $\left(\mathrm{NH}_{3}\right)$ and hydronium ion.
$\mathrm{NH}_{4}{ }^{+}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftarrows \mathrm{NH}_{3}(\mathrm{aq})+\mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})$


## Predicting Whether a Salt is Acidic, Basic, or Neutral

- These rules apply to normal salts (those in which the anion has no acidic hydrogen)

1. A salt of a strong base and a strong acid.

The salt has no hydrolyzable ions and so gives a neutral aqueous solution.

An example is NaCl .

## Predicting Whether a Salt is Acidic, Basic, or Neutral

- These rules apply to normal salts (those in which the anion has no acidic hydrogen)

2. A salt of a strong base and a weak acid.

The anion of the salt is the conjugate of the weak acid. It hydrolyzes to give a basic solution.

An example is NaCN .

## Predicting Whether a Salt is Acidic, Basic, or Neutral

- These rules apply to normal salts (those in which the anion has no acidic hydrogen)

3. A salt of a weak base and a strong acid.

The cation of the salt is the conjugate of the weak base. It hydrolyzes to give an acidic solution.

An example is $\mathrm{NH}_{4} \mathrm{Cl}$.

## Predicting Whether a Salt is Acidic, Basic, or Neutral

- These rules apply to normal salts (those in which the anion has no acidic hydrogen)

4. A salt of a weak base and a weak acid.

Both ions hydrolyze. You must compare the $\mathrm{K}_{\mathrm{a}}$ of the cation with the $\mathrm{K}_{\mathrm{b}}$ of the anion.
If the $\mathrm{K}_{\mathrm{a}}$ of the cation is larger the solution is acidic.
If the $\mathrm{K}_{\mathrm{b}}$ of the anion is larger, the solution is basic.

TABLE 14.5
Qualitative Prediction of pH for Solutions of Salts for Which Both Cation and Anion Have Acidic or Basic Properties

| $K_{\mathrm{a}}>K_{\mathrm{b}}$ | $\mathrm{pH}<7$ (acidic) |
| :--- | :--- |
| $K_{\mathrm{b}}>K_{\mathrm{a}}$ | $\mathrm{pH}>7$ (basic) |
| $K_{\mathrm{a}}=K_{\mathrm{b}}$ | $\mathrm{pH}=7$ (neutral) |

$\mathrm{pH}>7$ (basic)
$\mathrm{pH}=7$ (neutral)


## The pH of a Salt Solution

- To calculate the pH of a salt solution would require the $\mathrm{K}_{\mathrm{a}}$ of the acidic cation or the $K_{\mathrm{b}}$ of the basic anion.
- The ionization constants of ions are not listed directly in tables because the values are easily related to their conjugate species.
- Thus the $\mathbf{K}_{b}$ for $\mathbf{C N}^{-}$is related to the $\mathbf{K}_{\mathrm{a}}$ for HCN.


## The pH of a Salt Solution

- To see the relationship between $\mathrm{K}_{\mathrm{a}}$ and $\mathrm{K}_{\mathrm{b}}$ for conjugate acid-base pairs, consider the acid ionization of HCN and the base ionization of $\mathrm{CN}^{-}$.

| LeN $(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftarrows \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{CX}(\mathrm{aq})$ | $\mathrm{K}_{\mathrm{a}}$ |
| ---: | :--- |
| $\mathrm{aH}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftarrows \mathrm{HCN}^{2}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})$ | $\mathrm{K}_{\mathrm{b}}$ |
| $2 \mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftarrows \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})$ | $\mathrm{K}_{\mathrm{w}}$ |

- When these two reactions are added you get the ionization of water.


## The pH of a Salt Solution

- To see the relationship between $\mathrm{K}_{\mathrm{a}}$ and $\mathrm{K}_{\mathrm{b}}$ for conjugate acid-base pairs, consider the acid ionization of HCN and the base ionization of $\mathrm{CN}^{-}$.
$\omega \mathrm{K}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftarrows \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{CX}(\mathrm{aq}) \quad \mathrm{K}_{\mathrm{a}}$

| $\mathrm{AX}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftarrows \mathrm{HCN}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})$ |
| ---: |
| $2 \mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftarrows \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})$ |
| $\mathrm{K}_{\mathrm{w}}$ |

- When two reactions are added, their equilibrium constants are multiplied.


## The pH of a Salt Solution

- To see the relationship between $\mathrm{K}_{\mathrm{a}}$ and $\mathrm{K}_{\mathrm{b}}$ for conjugate acid-base pairs, consider the acid ionization of HCN and the base ionization of $\mathrm{CN}^{-}$.

| LeN $(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftarrows \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{CX}(\mathrm{aq})$ | $\mathrm{K}_{\mathrm{a}}$ |
| ---: | :--- |
| at $(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftarrows \mathrm{HN}^{2}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})$ | $\mathrm{K}_{\mathrm{b}}$ |
| $2 \mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftarrows \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})$ | $\mathrm{K}_{\mathrm{w}}$ |

- Therefore,

$$
\mathbf{K}_{\mathrm{a}} \times \mathbf{K}_{\mathrm{b}}=\mathbf{K}_{\mathrm{w}}
$$

## A Problem To Consider

- What is the pH of a 0.10 M NaCN solution at $25^{\circ} \mathrm{C}$ ? The $\mathrm{K}_{\mathrm{a}}$ for HCN is $4.9 \times 10^{-10}$.
- Sodium cyanide gives $\mathrm{Na}^{+}$ions and $\mathrm{CN}^{-}$ions in solution.
- Only the $\mathrm{CN}^{-}$ion hydrolyzes.
$\mathrm{CN}^{-}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \leftrightarrows \mathrm{HCN}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})$


## The pH of a Salt Solution

- For a solution of a salt in which only one ion hydrolyzes, the calculation of equilibrium composition follows that of weak acids and bases.
- The only difference is first obtaining the $\mathrm{K}_{\mathrm{a}}$ or $\mathrm{K}_{\mathrm{b}}$ for the ion that hydrolyzes.
- The next example illustrates the reasoning and calculations involved.


## A Problem To Consider

- What is the pH of a 0.10 M NaCN solution at $25^{\circ} \mathrm{C}$ ? The $\mathrm{K}_{\mathrm{a}}$ for HCN is $4.9 \times 10^{-10}$.
- The $\mathrm{CN}^{-}$ion is acting as a base, so first, we must calculate the $\mathrm{K}_{\mathrm{b}}$ for $\mathrm{CN}^{-}$.
$K_{b}=\frac{K_{w}}{K_{a}}=\frac{1.0 \times 10^{-14}}{4.9 \times 10^{-10}}=2.0 \times 10^{-5}$
- Now we can proceed with the equilibrium calculation.


## A Problem To Consider

- What is the pH of a 0.10 M NaCN solution at $25^{\circ} \mathrm{C}$ ? The $\mathrm{K}_{\mathrm{a}}$ for HCN is $4.9 \times 10^{-10}$.
- Let $x=\left[\mathrm{OH}^{-}\right]=[\mathrm{HCN}]$, then substitute into the equilibrium expression.
$\frac{[\mathrm{HCN}]\left[\mathrm{OH}^{-}\right]}{\left[\mathrm{CN}^{-}\right]}=\mathrm{K}_{\mathrm{b}}$


## A Problem To Consider

- What is the pH of a 0.10 M NaCN solution at $25^{\circ} \mathrm{C}$ ? The $\mathrm{K}_{\mathrm{a}}$ for HCN is $4.9 \times 10^{-10}$.
- This gives

$$
\frac{x^{2}}{(0.10-x)}
$$

## Structure and Acid-Base Properties

- Two factors for acidity in binary compounds:

Bond Polarity (high is good)

Bond Strength (low is good)

- As expected, the solution has a pH greater than 7.0.


## Molecular Structure and Acid Strength

- Two factors are important in determining the relative acid strengths.
- One is the polarity of the bond to which the hydrogen atom is attached.
- The H atom should have a partial positive charge:

- The more polarized the bond, the more easily the proton is removed and the greater the acid strength.


## Molecular Structure and Acid

 Strength- Two factors are important in determining the relative acid strengths.
- The second factor is the strength of the bond. Or, in other words, how tightly the proton is held.
- This depends on the size of atom X.

$$
\stackrel{\delta+}{\mathbf{H}}-\stackrel{\delta-}{\mathbf{X}}
$$

- The larger atom X , the weaker the bond and the greater the acid strength.


## Molecular Structure and Acid Strength

- Consider a series of binary acids from a given column of elements.
- As you go down the column of elements, the radius increases markedly and the $\mathrm{H}-\mathrm{X}$ bond strength decreases.
- You can predict the following order of acidic strength.

$$
\mathrm{HF}<\mathrm{HCl}<\mathrm{HBr}<\mathrm{HI}
$$

## Molecular Structure and Acid Strength

- As you go across a row of elements, the polarity of the $\mathrm{H}-\mathrm{X}$ bond becomes the dominant factor.
- As electronegativity increases going to the right, the polarity of the $\mathrm{H}-\mathrm{X}$ bond increases and the acid strength increases.
- You can predict the following order of acidic strength.

$$
\mathrm{H}_{3} \mathrm{~N}<\mathrm{H}_{2} \mathrm{O}<\mathbf{H F}
$$

## Molecular Structure and Acid Strength

- Consider the oxoacids. An oxoacid has the structure:

$$
\mathrm{H}-\mathrm{O}-\mathrm{Y}-
$$

- The acidic H atom is always attached to an O atom, which in turn is attached to another atom Y .
- Bond polarity is the dominant factor in the relative strength of oxoacids.
- This, in turn, depends on the electronegativity of the atom Y .


## Molecular Structure and Acid Strength

- Consider the oxoacids. An oxoacid has the structure:

$$
\mathrm{H}-\mathrm{O}-\mathrm{Y}
$$

- If the electronegativity of Y is large, then the $\mathrm{O}-\mathrm{H}$ bond is relatively polar and the acid strength is greater.
- We can predict the acid strength for compounds with Y in the same group:
$\mathrm{HOCl}>\mathrm{HOBr}>\mathrm{HOI}$

TABLE 14.9 Comparison of Electronegativity of $X$ and $K_{a}$ Value for a Series of Oxyacids

| Acid | Electronegativity <br> of X |  |  |  | $K_{\mathrm{a} \text { for Acid }}$ |
| :--- | :--- | :--- | :---: | :---: | :---: |
| HOCl | Cl | 3.0 | $4 \times 10^{-8}$ |  |  |
| HOBr | Br | 2.8 | $2 \times 10^{-9}$ |  |  |
| HOI | I | 2.5 | $2 \times 10^{-11}$ |  |  |
| $\mathrm{HOCH}_{3}$ | $\mathrm{CH}_{3}$ | 2.3 (for carbon in $\mathrm{CH}_{3}$ ) | $\sim 10^{-15}$ |  |  |

## Molecular Structure and Acid Strength

- Consider the oxoacids. An oxoacid has the structure:

$$
\mathrm{H}-\mathrm{O}-\mathrm{Y}-\mathrm{X}
$$

- Other groups, such as O atoms or $\mathrm{O}-\mathrm{H}$ groups, may be attached to Y .
- With each additional O atom, Y becomes effectively more electronegative.


## Molecular Structure and Acid Strength

- Consider the oxoacids. An oxoacid has the structure:

$$
\mathrm{H}-\mathrm{O}-\mathrm{Y}-
$$

- As a result, the H atom becomes more acidic.
- The acid strengths of the oxoacids of chlorine increase in the following order.

$$
\mathrm{HClO}<\mathrm{HClO}_{2}<\mathrm{HClO}_{3}<\mathrm{HClO}_{4}
$$



## Molecular Structure and Acid Strength

- Consider polyprotic acids and their corresponding anions.
- Each successive H atom becomes more difficult to remove.
- Therefore the acid strength of a polyprotic acid and its anions decreases with increasing negative charge.

$$
\mathrm{HPO}_{4}{ }^{2-}<\mathrm{H}_{2} \mathrm{PO}_{4}^{-}{ }^{-}<\mathrm{H}_{3} \mathrm{PO}_{4}
$$

## Oxides

- Acidic Oxides (Acid Anhydrides):
( $\mathrm{O}-\mathrm{X}$ bond is strong and covalent.

$$
\cdot \mathrm{SO}_{2}, \mathrm{NO}_{2}, \mathrm{CrO}_{3}
$$

- Basic Oxides (Basic Anhydrides):
(1) $\mathrm{O}-\mathrm{X}$ bond is ionic.

$$
\text { - } \mathrm{K}_{2} \mathrm{O}, \mathrm{CaO}
$$

## Lewis Acids and Bases

- Lewis Acid: electron pair acceptor
- Lewis Base: electron pair donor


TABLE 14.10 Three Models for Acids and Bases

| Model | Definition of Acid | Definition of Base |
| :--- | :--- | :--- |
| Arrhenius | $\mathrm{H}^{+}$producer | $\mathrm{OH}^{-}$producer |
| Brønsted-Lowry | $\mathrm{H}^{+}$donor | $\mathrm{H}^{+}$acceptor |
| Lewis | Electron-pair acceptor | Electron-pair donor |

## Lewis Concept of Acids and Bases

- The Lewis concept defines an acid as an electron pair acceptor and a base as an electron pair donor.
- This concept broadened the scope of acid-base theory to include reactions that did not involve $\mathrm{H}^{+}$.
- The Lewis concept embraces many reactions that we might not think of as acid-base reactions.

$$
\mathrm{Al}^{3+}+6 \mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{Al}\left(\mathrm{OH}_{2}\right)_{6}{ }^{3+}
$$

A model of
$\mathrm{A}\left(\mathrm{OH}_{2}\right)_{6}{ }^{3+}$.
A lone pair from the oxygen atom in each water molecule is donated to the $\mathrm{Al}^{3+}$ to coordinate covalent bonds between the water molecules and

$\mathrm{Al}\left(\mathrm{OH}_{2}\right)_{6}{ }^{3+}$ aluminum ion

