# Scattering

Nuclear Physics 415/515
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## What Do we Need?

- Beam
- Electrons or muons  $\rightarrow \gamma^*$ ; pions, protons, antiprotons, light nuclei, heavy ions...
- Targets (or counterrotating beams)
- Protons, deuterons, <sup>3</sup>He, heavier nuclei, heavy ions, antiprotons
- Detectors
- For scattered/produced electrons/muons/... and hadrons/nuclei
- **Facilities**





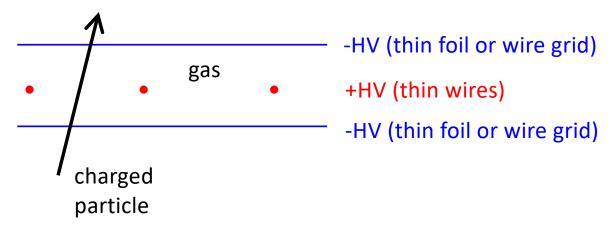






### Typical Detector Elements

Wire chambers measure position (and angle)



- 1. Charged particle passes through wire chamber and knocks out electrons from the gas.
- Electrons drift in the E field to the cathode wire, colliding with gas molecules
- 3. Close to the wire, the mean free path times the electric field is large enough to ionize the gas molecules. Avalanche!
- 4. Read the signal on the cathode wire (time gives distance) Similar:  $G_{as}E_{lectron}M_{ultiplier}S$ ,  $\mu MEGAS$ ,...

Applications: VDC, Multi-layer drift chamber (track  $\rightarrow$  ),  $\overrightarrow{Tp}_{e}$ Projection Chamber

#### **Typical Detector Elements**

Scintillators: time ( $\Rightarrow \beta \Rightarrow$  particle type) and energy measurement (typical resolution: down to 50-100 ps for plastic)

- Typically a doped plastic or crystal (eg: Ge, NaI, BaF<sub>2</sub>)
- Charged particle passes through scintillator (or neutral particle interacts) and excites atomic electrons. These de-excite and emit light.
- Minimum energy loss (when  $\beta \gamma \approx 1$ ) is dE/dx = 2 MeV/(g/cm<sup>2</sup>)

Cherenkov counter: threshold velocity measurement.

- Typically an empty box with smoke (ie: a gas) and mirrors
- Local light speed is v = 1/n < c
- Particles travelling faster than v will emit Cherenkov light
   (an electromagnetic 'sonic boom') ⇒ threshold CC (yes/no)
- The opening angle of the Cherenkov cone is related to the particle's velocity  $\Rightarrow R_{ing}I_{maging}CH_{erenkov}$  (measure  $\beta \Rightarrow$  particle type)

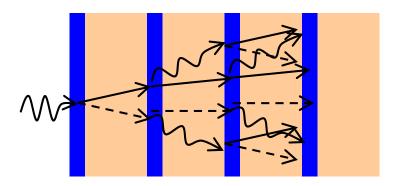
Also: Transition Radiation Detector, DIRC,

#### Photon Counters ->

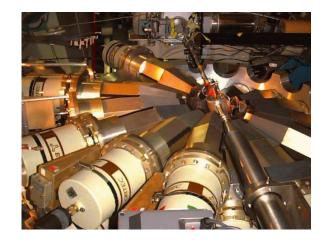
#### Electromagnetic shower counters:

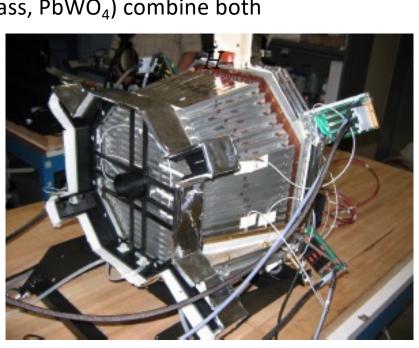
measure energy (+ time), discriminate electrons and detect neutral particles

- Electrons and photons passing through material shower
- After one radiation length of material on average:
  - Electrons emit a bremsstrahlung photon
  - Photons convert to an electron/positron pair or Compton-scatter
- After  $\approx 10$  radiation lengths, one e<sup>-</sup> or  $\gamma$  is now  $\approx 1000$  particles
- Simple design: alternating layers of lead ( $R_L = 6$  mm) and scintillant Higher resolution: Heavy metal glass (Pb glass, PbWO<sub>4</sub>) combine both
  - Particles shower in the lead
  - •Charged particles deposit energy in the scintillant



Also: Hadronic Calorimeter, μ counter...

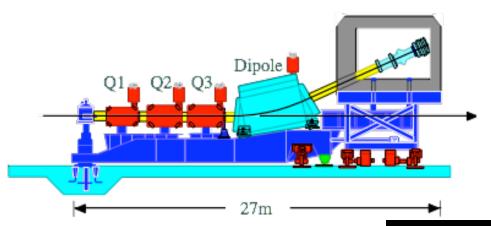




# Detectors+Magnets = Spectrometers

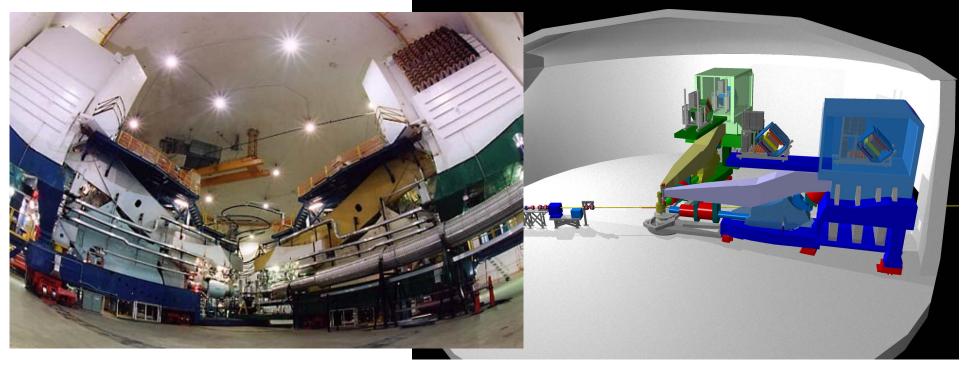


SLAC End Station A – where the quarks were discovered experimentally

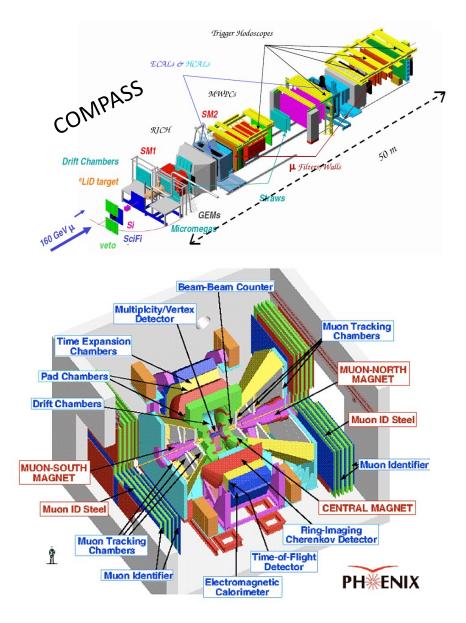


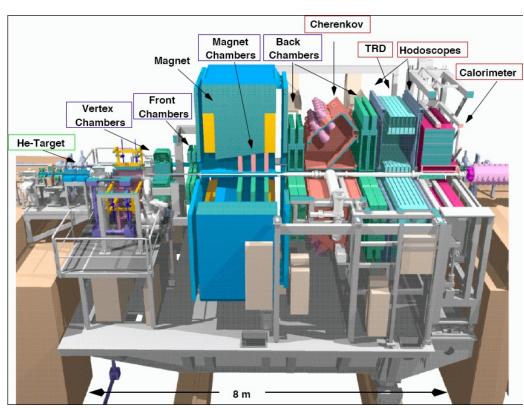
### Jefferson Lab Hall A (Hall C similar)

Typically, small acceptance but high resolution, very good shielding (→ high luminosity)

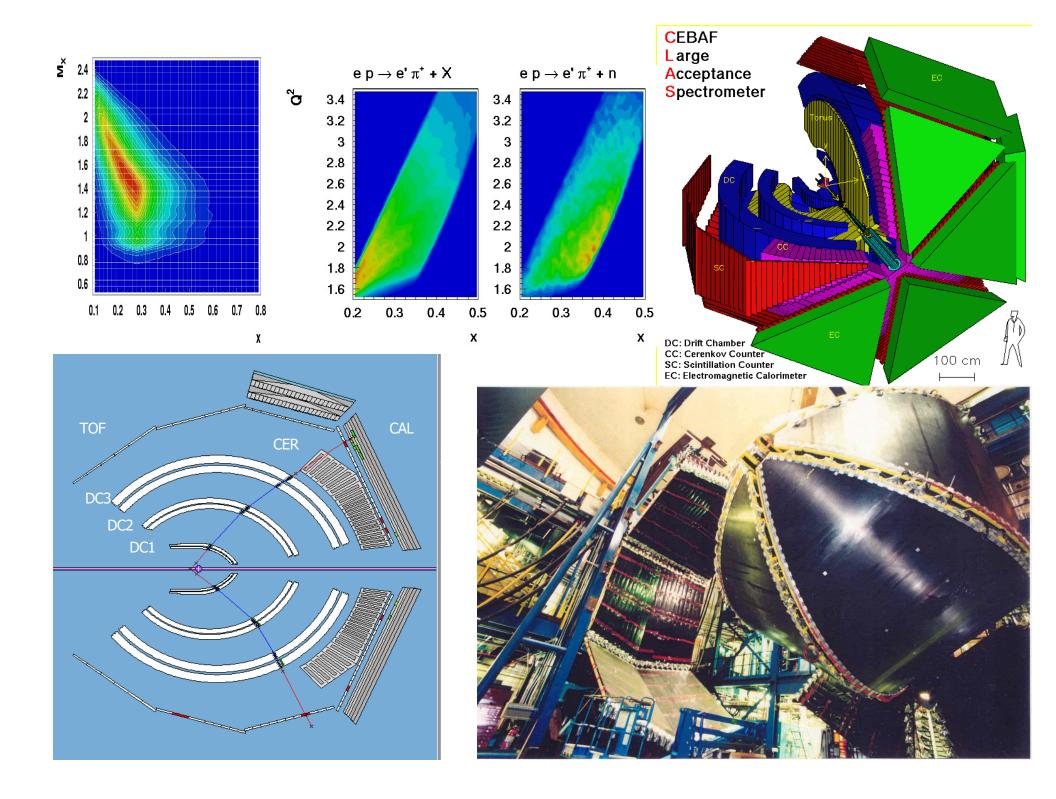


# Large Acceptance Spectrometers





**HERMES** 



## CLAS12

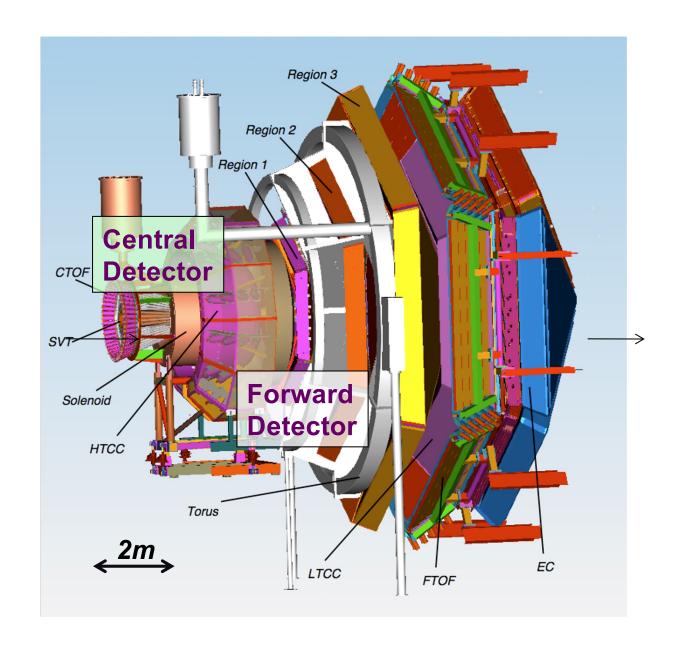
#### Another nearly $4\pi$ detector in Hall D (GLUEX)

#### **Base equipment**

- Forward Detector
- TORUS magnet
- Forward vertex tracker
- HT Cherenkov Counter
- Drift chamber system
- LT Cherenkov Counter
- Forward ToF System
- Preshower calorimeter
- E.M. calorimeter
- Central Detector
- SOLENOID magnet
- Barrel Silicon Tracker
- Central Time-of-Flight

#### **Additional equipment**

- Micromegas (CD & FD)
- RICH counter (FD)
- Neutron detector (CD)
- Small angle tagger (FD)



## Cross Section and Reaction Rate

- Incoming "current":  $\dot{n}_b$  (beam particles/s)
- Target areal density:  $n_T L$  = number of nuclei per unit surface area
- Cross section  $\Delta \sigma$  for a specific reaction to happen
- => number of times this reaction happens per second (event rate):  $\dot{N} = \dot{n}_b n_T L \Delta \sigma$
- Call  $\downarrow = \dot{n}_b n_T L$  the luminosity of the experiment

$$N = \int \Delta \sigma \, dt$$

# Example: Luminosity and cross sections

- On white board
- Remember: If atomic mass is A, then 1 g of the material contains 1/A mol
- 1 mol =  $6.022 \cdot 10^{23}$  atoms (and hence nuclei)
- 1µA of electrons contain  $10^{-6} \, ^{\text{C}}/_{\text{s}} / 1.6 \cdot 10^{-19} \, \text{C} = 6.25 \cdot 10^{12} \, \text{e/s}$
- 1 "barn" 1 b =  $10^{-24}$  cm<sup>2</sup>
  - mb(arn), μb, nb, pb,...

# Example partial cross section: scattering into a detector

Look only at events where the beam particle is

 $\Delta\Omega = A_D/r^2$ 

Target plane

scattered into a specific detector area = a specific angular range in  $\theta$  and  $\phi$  => Solid angle  $\Delta\Omega$ 

 $\Delta \sigma$  proportional to  $\Delta \Omega$ 

=> Use ratio  $\Delta \sigma / \Delta \Omega$  to express the "intrinsic" scattering strength (independent of detector used)

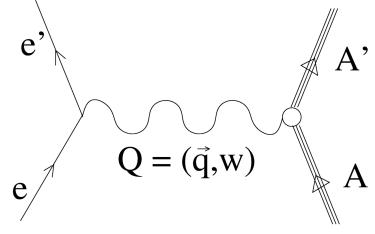
$$\dot{N}(E, \theta, \Delta\Omega) = \mathcal{L} \cdot \frac{\mathrm{d}\sigma(E, \theta)}{\mathrm{d}\Omega} \Delta\Omega$$

# Why use electrons and photons?

- Probe structure understood (point particles)
- Electromagnetic interaction understood (QED)
- Interaction is weak ( $\alpha = 1/137$ )
  - Perturbation theory works!
    - First Born Approx / one photon exchange
  - Probe interacts only once
  - Study the entire nuclear volume

#### **BUT:**

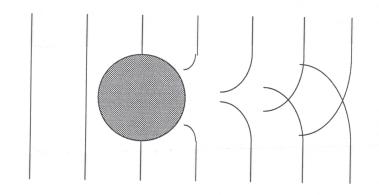
- Cross sections are small
- Electrons radiate



## **Electrons as Waves**

Scattering process is quantum mechanical

$$\lambda = \frac{h}{p}$$



Electron energy:

$$E_e \approx pc$$

# **Experimental goals:**

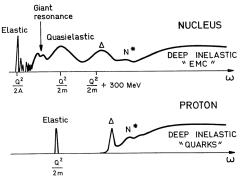
- Elastic scattering
  - structure of the nucleus
    - Form factors, charge distributions, spin dependent FF



- Shell structure
  - Momentum distributions
  - Occupancies
- Short Range Correlated nucleon pairs
- Nuclear transparency and color transparency

## Deep Inelastic Scattering (DIS)

- The EMC Effect and Nucleon modification in nuclei
- Quark hadronization in nuclei



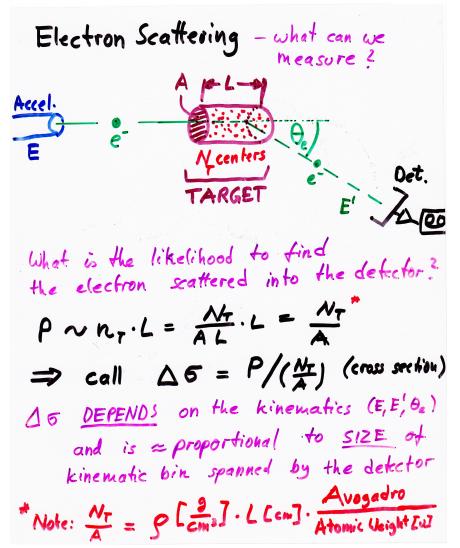
# Energy vs length

Select spatial resolution and excitation energy independently

- Photon energy v determines excitation energy
- Photon momentum q determines spatial resolution:  $\lambda \approx \frac{\hbar}{-}$

#### Three cases:

- Low q
  - Photon wavelength  $\lambda$  larger than the nucleon size ( $R_{\rm p}$ )
- Medium q: 0.2 < q < 1 GeV/c
  - $-\lambda \sim R_{\rm p}$
  - Nucleons resolvable
- High q: q > 1 GeV/c
  - $-\lambda < R_{\rm p}$
  - Nucleon structure resolvable



Count rate (L = luminosity):

$$\dot{N} = P \cdot \dot{n}_{el} = \Delta \sigma \cdot \frac{N_T}{A} \dot{n}_{el} = \Delta \sigma \cdot \frac{N_T}{A} \frac{I}{e} = \Delta \sigma \cdot L$$

In general:

$$\Delta \sigma = \Delta \sigma \left( E'...E' + \Delta E', \theta_e...\theta_e + \Delta \theta_e, \varphi...\varphi + \Delta \varphi \right)$$

Limit of infinitesimal acceptance:

$$\Delta \sigma = \frac{d^3 \sigma}{dE' d\theta_e d\varphi} (E', \theta_e, \varphi) \Delta E' \Delta \theta_e \Delta \varphi = \frac{d\sigma}{dE' d\Omega} \Delta E' \Delta \Omega$$

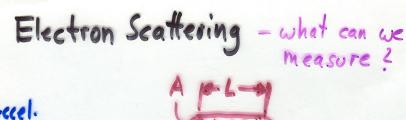
(use Jacobian to transform variables)

In case of more particles/observables and finite phase space:

$$\Delta \sigma = \iint\limits_{\substack{Phase \\ Space}} \frac{d^n \sigma}{dk_1 dk_2 ... dk_n} (k_1 ... k_n) Acc(k_1 ... k_n) dk_1 dk_2 ... dk_n$$

where Acceptance is defined by detector boundaries and bin sizes as well as number of observed particles

(inclusive = only 1, semi-inclusive, exclusive)





What is the likelihood to find the electron scattered into the detector?

$$\Rightarrow$$
 call  $\Delta 6 = P/(\frac{M}{4})$  (cross section)

 $\Delta \delta$  <u>DEPENDS</u> on the kinematics (E, E,  $\theta_e$ ) and is  $\approx$  proportional to <u>SIZE</u> of kinematic bin spanned by the detector

What is the transition rate

$$\dot{N}_{e,f} = \dot{N}_{e,in} \cdot P(i \rightarrow f) = I_{e,in} \cdot \frac{N_T}{A} \cdot \Delta \delta$$

$$= \frac{I_{e,in}}{A} \cdot N_T \cdot \Delta \delta = (\overrightarrow{J}_{e,in}) \cdot N_T \cdot \Delta \delta$$

Fermi's GOLDEN Rule:

$$W_{i} \rightarrow f = \frac{2\pi}{\hbar} |M_{fi}|^2 \Delta \phi$$

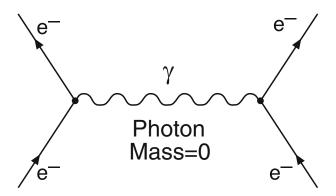
Phase space spanned by de kecher/kinsmalichi

 $M_{fi} = \langle \psi_f | H_{in} + | \psi_{in} \rangle$ 

# How do we calculate cross sections? Feynman diagrams

- Theoretical ansatz: Look at single scattering centers, incoming beam = current density  $j_b$ . Event rate  $\dot{N} = \Delta \sigma^{.} j_b$ .
- "Infinitesimal" cross section:  $d\sigma/d\Omega(\theta,\phi)$ .
- Differential cross section depends only on physics of interaction (potential...) and available final state "phase space".
- Interaction often depicted with Feynman diagrams.

$$\sigma = \frac{2\pi}{\hbar \cdot v_a} \left| \mathcal{M}_{fi} \right|^2 \cdot \varrho \left( E' \right)$$



# Recap: Relativistic Kinematics

- Often in high energy nuclear/particle physics, particles move with close to the speed of light, c, hence we have to use special relativity
- Recall:  $\gamma = (1-v^2/c^2)^{-1/2}$ ,  $\beta = v/c$ ,  $E = \gamma Mc^2$ ,  $p = \gamma Mv$ . (Note: we'll simplify our lives by often ignoring factors of c.)
- 4-vectors:  $v^{\mu} = (v^0, v^1, v^2, v^3)$ .  $x^{\mu} = (ct, x, y, z)$ .  $P^{\mu} = (E/c, \vec{p})$  ( $\vec{p} =$  "3-vector part" of  $P^{\mu}$ ).
- General transformation: Lorentz Matrix
- Very useful in relativistic kinematics: Invariants (same in all coordinate systems). *E.g.*: Scalar product  $P^{\mu} P_{\mu} = (P^0)^2 \vec{p}^2 = M^2 c^2$ .