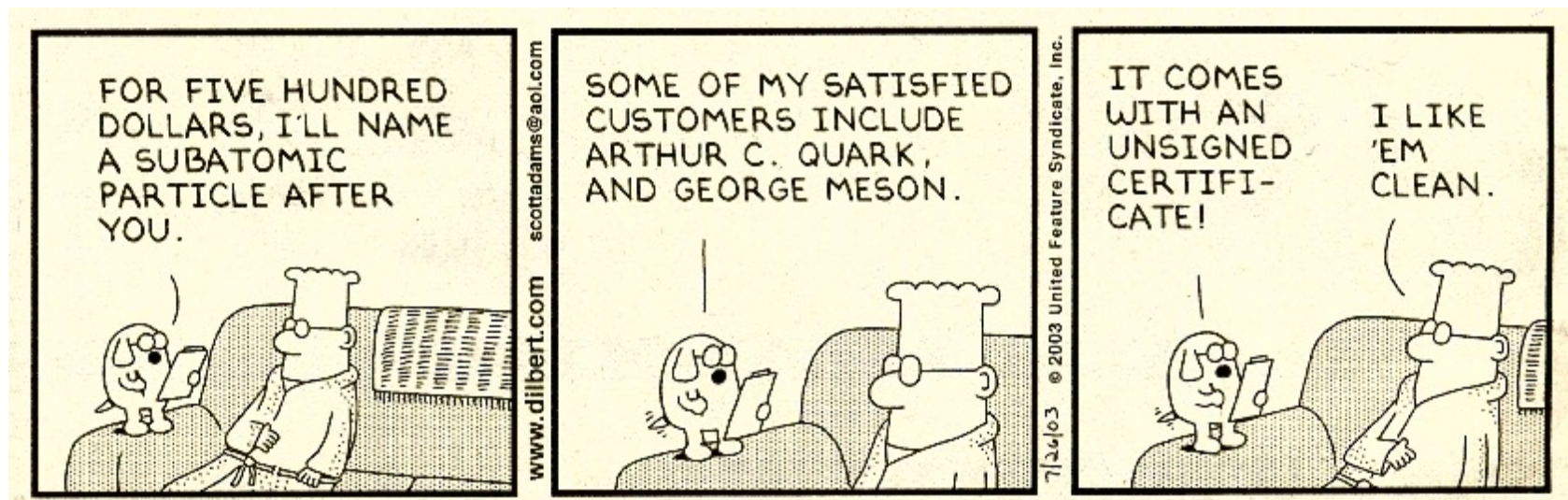


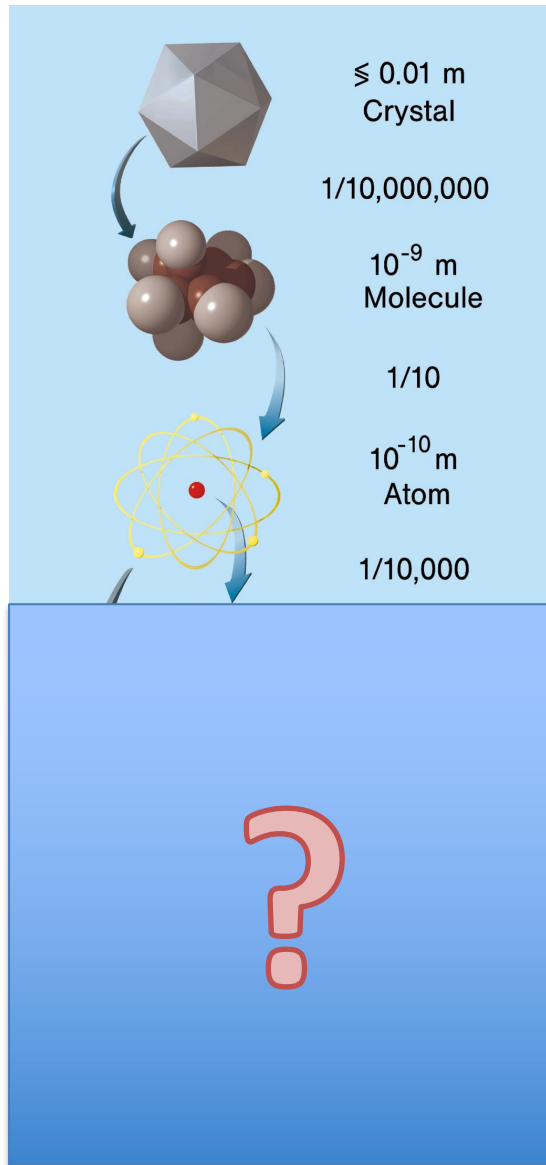
# PHYS415/515:

## Particle and Nuclear Physics

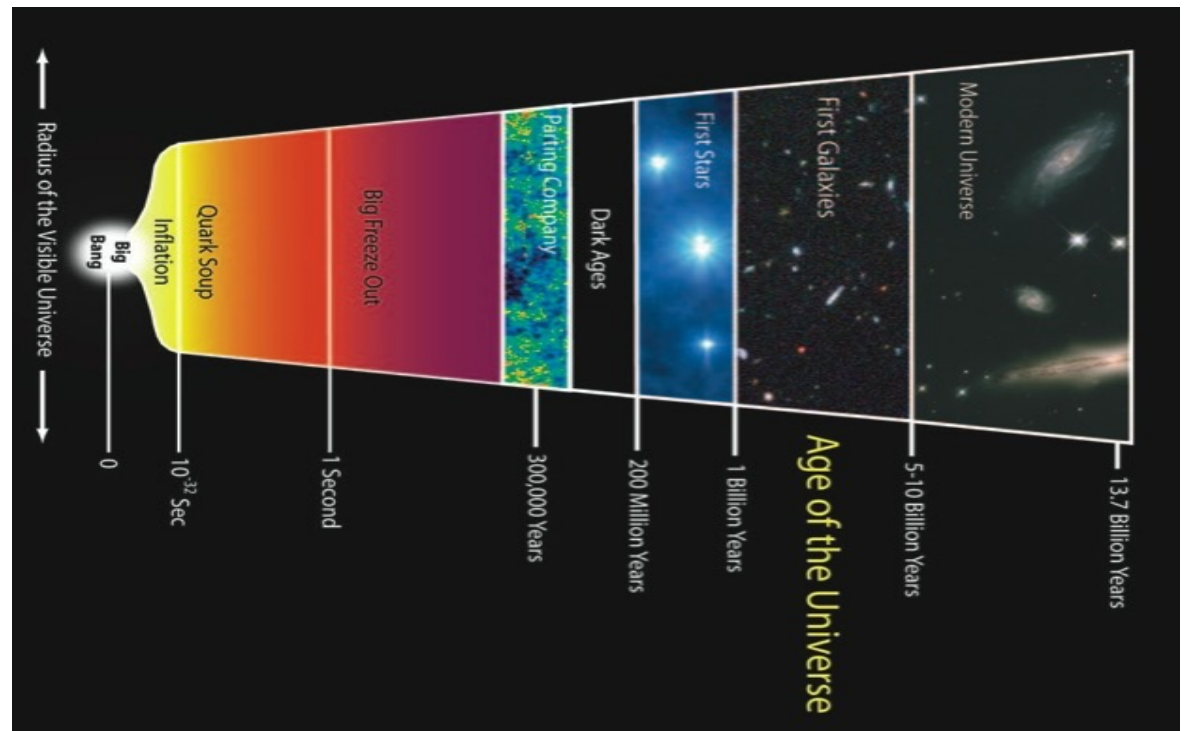
Sebastian Kuhn



# The Structure of Matter



- What is the Universe made off?
- What are the most fundamental objects in Nature?
- What particles were there in the beginning (right after the big bang)?
- How do they interact? How do they form larger objects?
- Where does all matter in the present Universe come from?



# Hydrogen Atom Wave functions

Remember Modern Physics / QM?

When  $n=1, l=0, m=0$  : 1s  $\Psi_{1,0,0} = \sqrt{\frac{1}{a_0^3 \pi}} e^{-r/a_0}$

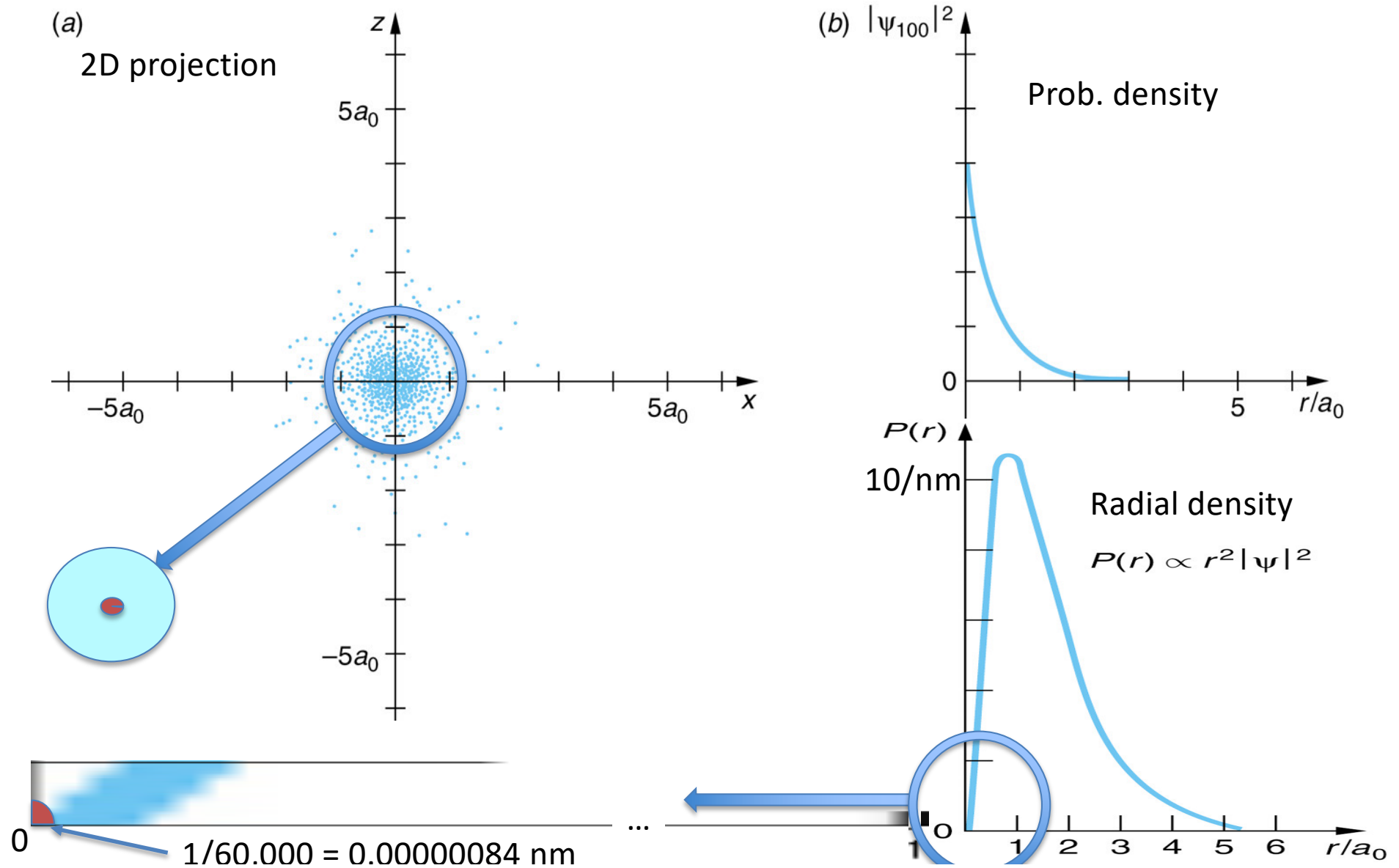
$n=2, l=0, m=0$  : 2s  $\Psi_{2,0,0} = \sqrt{\frac{1}{32a_0^3 \pi}} \left(2 - \frac{r}{a_0}\right) e^{-r/2a_0}$

$l=1, m=0, \pm 1$  : 2p  $\Psi_{2,1,0} = \sqrt{\frac{1}{32a_0^3 \pi}} \frac{r}{a_0} \cos \theta e^{-r/2a_0}$ ,  $\Psi_{2,1,\pm 1} = \mp \sqrt{\frac{1}{64a_0^3 \pi}} \frac{r}{a_0} \sin \theta e^{\pm i\varphi} e^{-r/2a_0}$

$$a_0 = \frac{4\pi\epsilon_0 \hbar^2}{e^2 m_e} = \frac{\hbar}{m_e c \alpha} = 0.0529 \text{ nm} \approx 0.53 \text{ \AA}$$

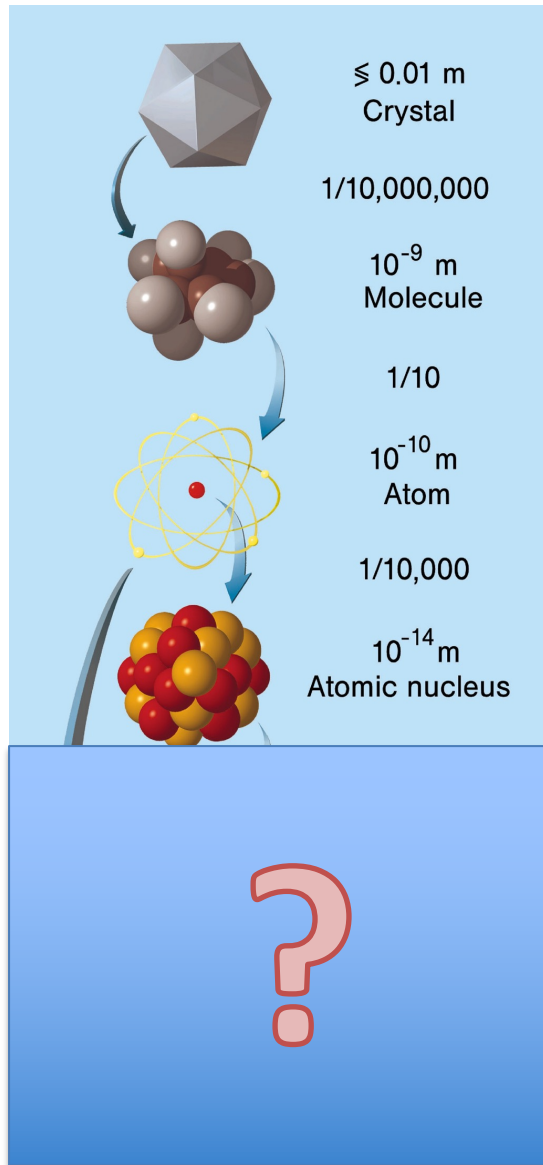
- $\hbar$  is the **reduced Planck constant**,  $\approx 197.33 \frac{\text{nm eV}}{c}$
- $m_e$  is the **mass of an electron**,  $\approx 511 \text{ keV}/c^2$
- $e$  is the **elementary charge**,
- $c$  is the **speed of light** in vacuum, and
- $\alpha$  is the **fine-structure constant**.  $\approx 1/137.036$

# H ground state

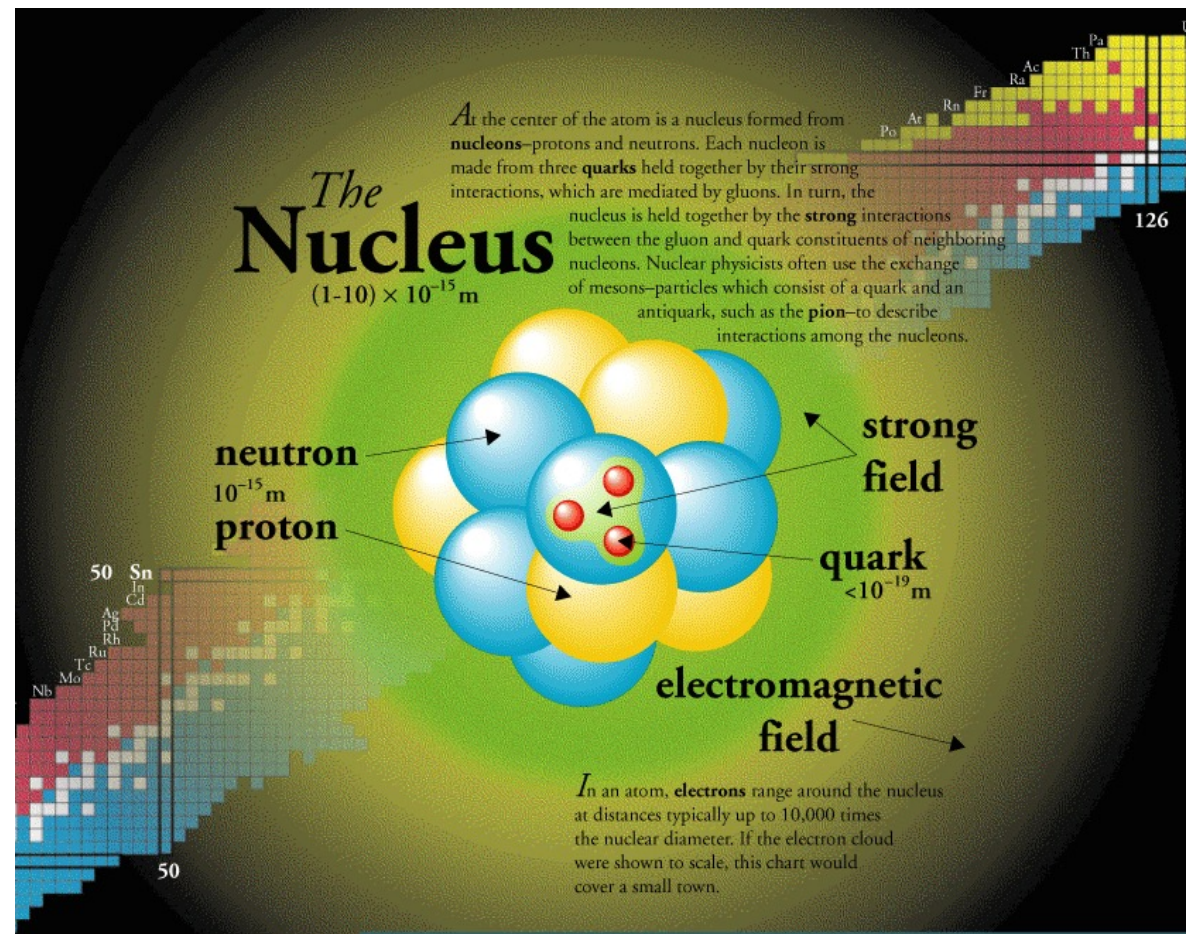




# The Structure of Matter



99.97% of the mass of an atom (and hence of all visible matter) is concentrated in the nucleus.  
 0.000,000,000,024% of the atomic volume is occupied by the nucleus .



# Stable nuclei

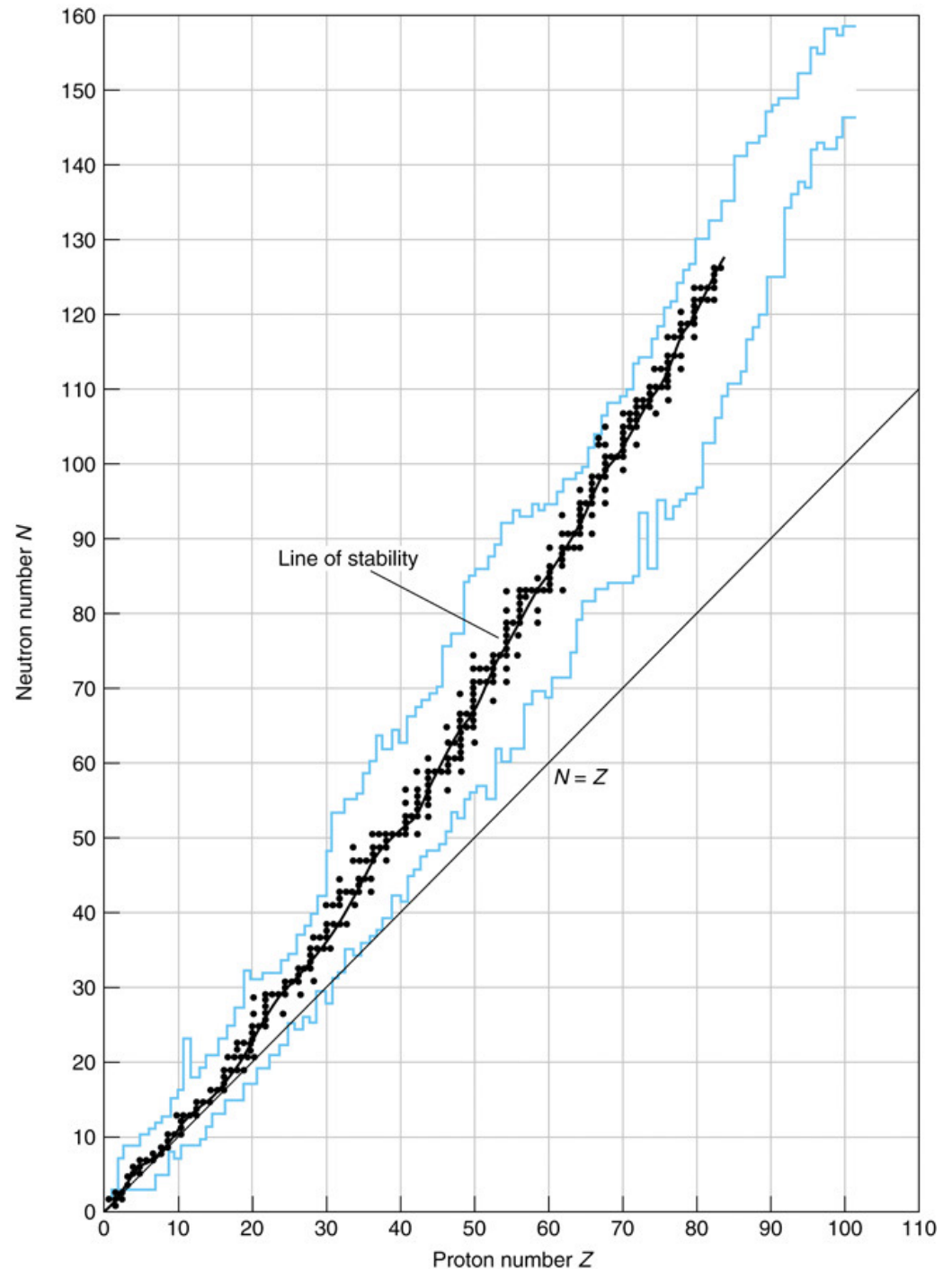
$A = N + Z$  (all integers)

Isotopes: SAME  $Z$

Isobars: SAME  $A$

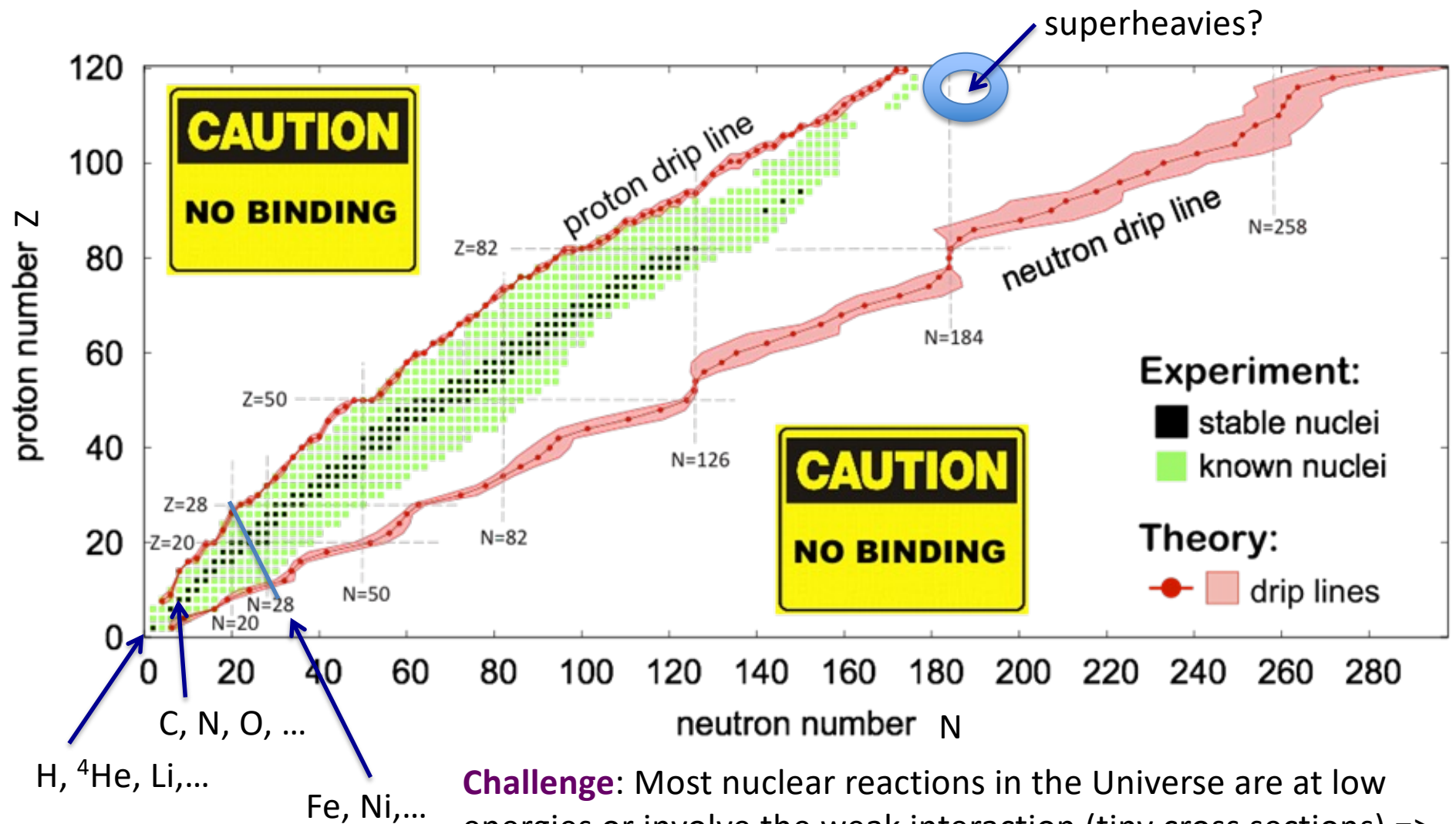
Nuclear mass is ROUGHLY  
proportional to  $A$  (see later)

ATOMIC mass can be fractional if  
the natural abundance of a given  
element has several stable  
isotopes



# All the nuclei in the universe

n stars



**Challenge:** Most nuclear reactions in the Universe are at low energies or involve the weak interaction (tiny cross sections) => Experiments and Theory are HARD! (subtle effects play big role!)

## Atomic Binding energy

$$B_{\text{atomic}} = M_{\text{At}}c^2 - M_{\text{Nuc}}c^2 - Z \cdot m_e c^2$$

$M_{\text{Nuc}}$  = Mass of Nucleus

$M_{\text{At}}$  = Atomic mass (single isotope)

Z = Element Number

Typical values: few  
eV's ... keV's

## Nuclear Binding energy

$$B_{\text{nuclear}} = M_{\text{N}}c^2 - Z \cdot m_p c^2 - N \cdot m_n c^2$$

$m_p$  = Mass of Proton

$m_n$  = Mass of neutron

$$A = N + Z$$

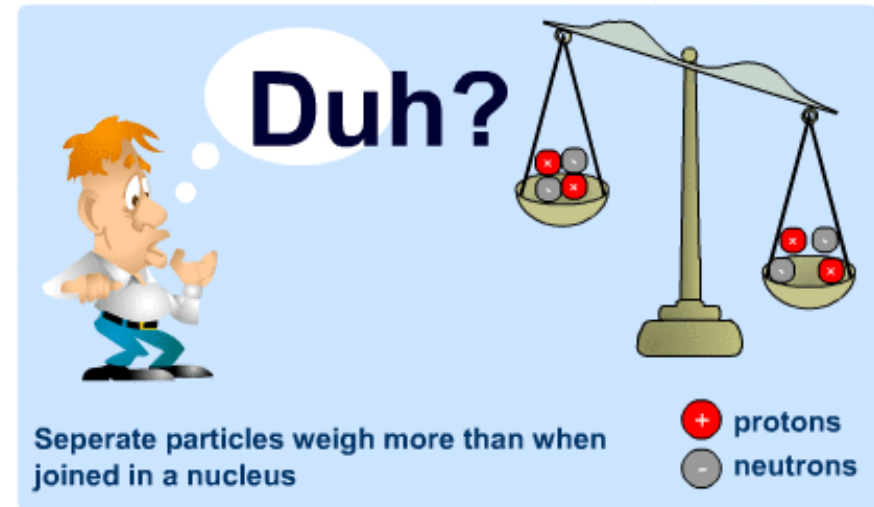
A = Atomic Mass Number

N = Neutron Number

Z = Proton Number

Typical values: keV's to 100's of MeV's

$$E = mc^2$$



In atomic and nuclear physics, masses are typically given in atomic mass units (u)  $1\ u = 1.66054 \times 10^{-27}\ \text{kg} = 931.494\ \text{MeV}/c^2$

Proton = 938.27 MeV  
Neutron = 939.51 MeV

$^2\text{H}$  components

1.007276 amu ●+

1.008665 amu ●-

0.000549 amu ●-

---

2.016490 amu

$^2\text{H}$  atom




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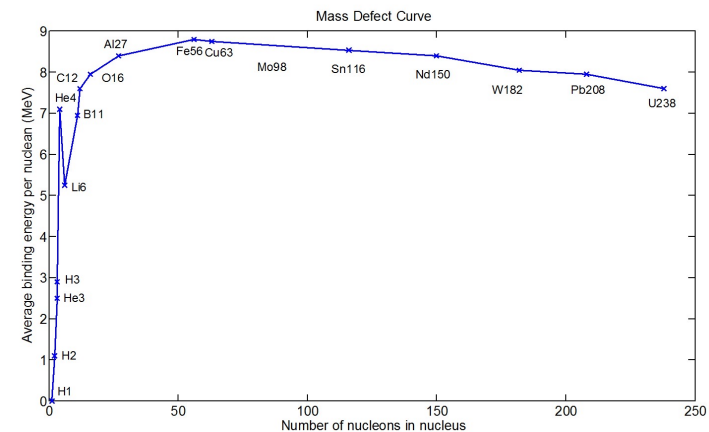
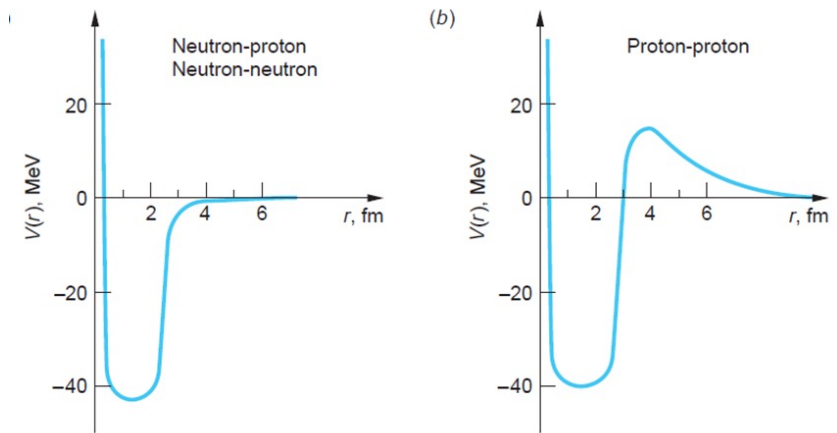
2.014102 amu

Mass defect = 0.002388 amu = 2.224 MeV

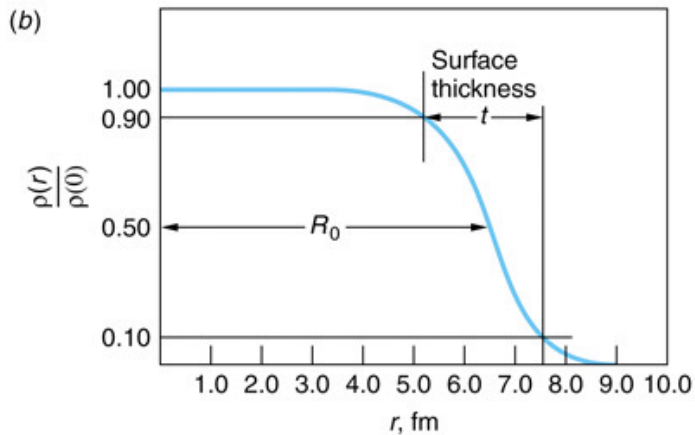
Note:  $amu = u$  (depending on who is talking)

# Nuclear Force

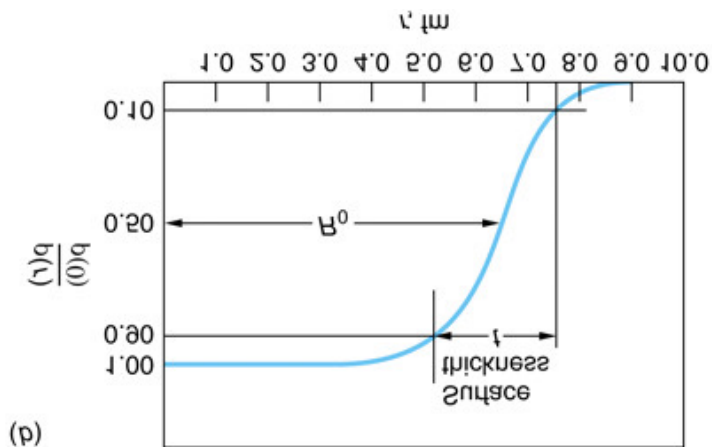
- Charge independent.
- Highly dependent on distance
- Saturated force
- Coulomb Repulsion will overcome the Nuclear Force as atoms become larger.



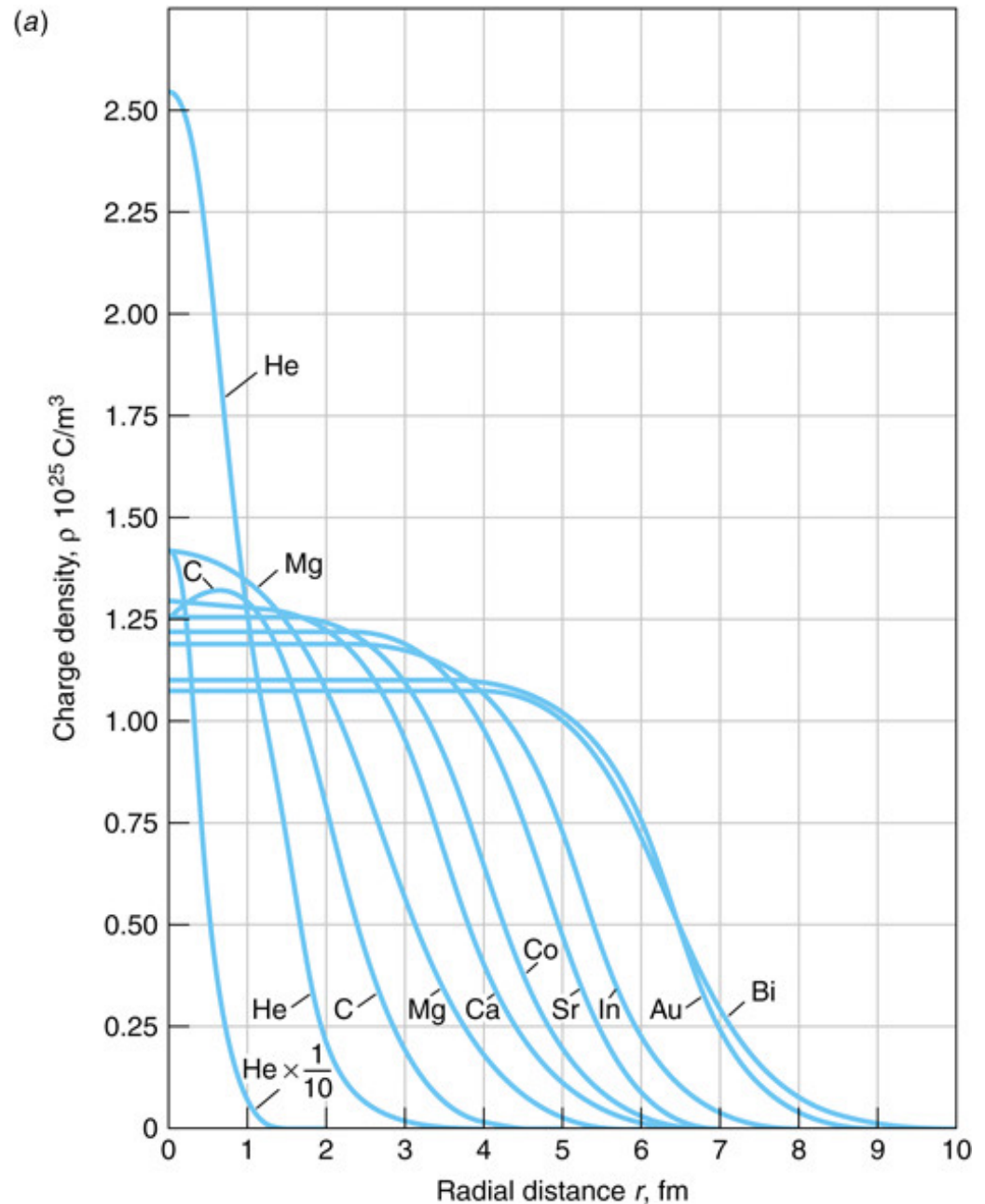
# Nuclear Density



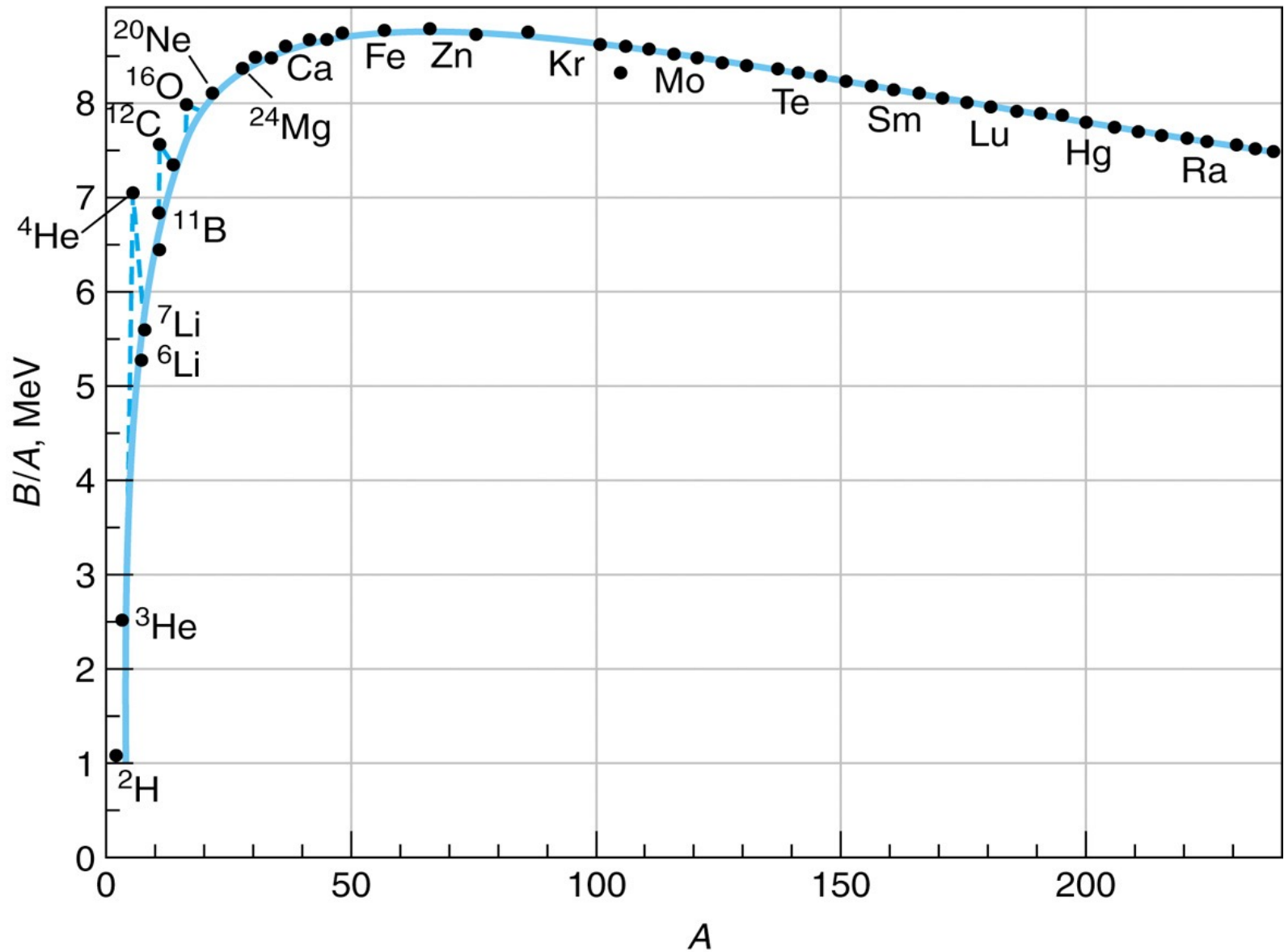
Typical Nuclear Density Profile  
(Cesium?)



=> Due to short range nuclear force,  
each nucleon "sees" THIS potential



# Nuclear Binding energies



# Liquid Drop Model

From previous slides, we find that nuclear density is roughly constant, and hence the nuclear radius goes like  $A^{1/3}$

$$R = 1.22 \text{ fm} \cdot A^{1/3}$$

$$\text{Surface} = 19 \text{ fm}^2 \cdot A^{2/3}$$

$$M(A, Z) = NM_n + ZM_p + Zm_e - a_v A + a_s A^{2/3} + a_c \frac{Z^2}{A^{1/3}} + a_a \frac{(N - Z)^2}{4A} + \frac{\delta}{A^{1/2}}$$

$$a_v = 15.67 \text{ MeV}/c^2$$

$$a_s = 17.23 \text{ MeV}/c^2$$

$$a_c = 0.714 \text{ MeV}/c^2$$

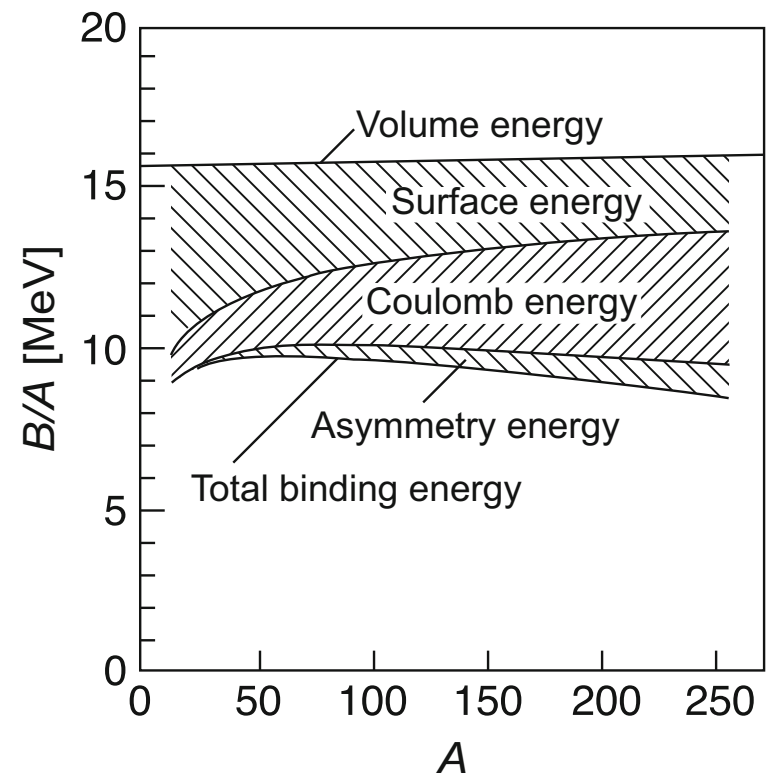
$$a_a = 93.15 \text{ MeV}/c^2$$

$$\delta = \begin{cases} -11.2 \text{ MeV}/c^2 & \text{for even } Z \text{ and } N \text{ (even-even nuclei)} \\ 0 \text{ MeV}/c^2 & \text{for odd } A \text{ (odd-even nuclei)} \\ +11.2 \text{ MeV}/c^2 & \text{for odd } Z \text{ and } N \text{ (odd-odd nuclei).} \end{cases}$$

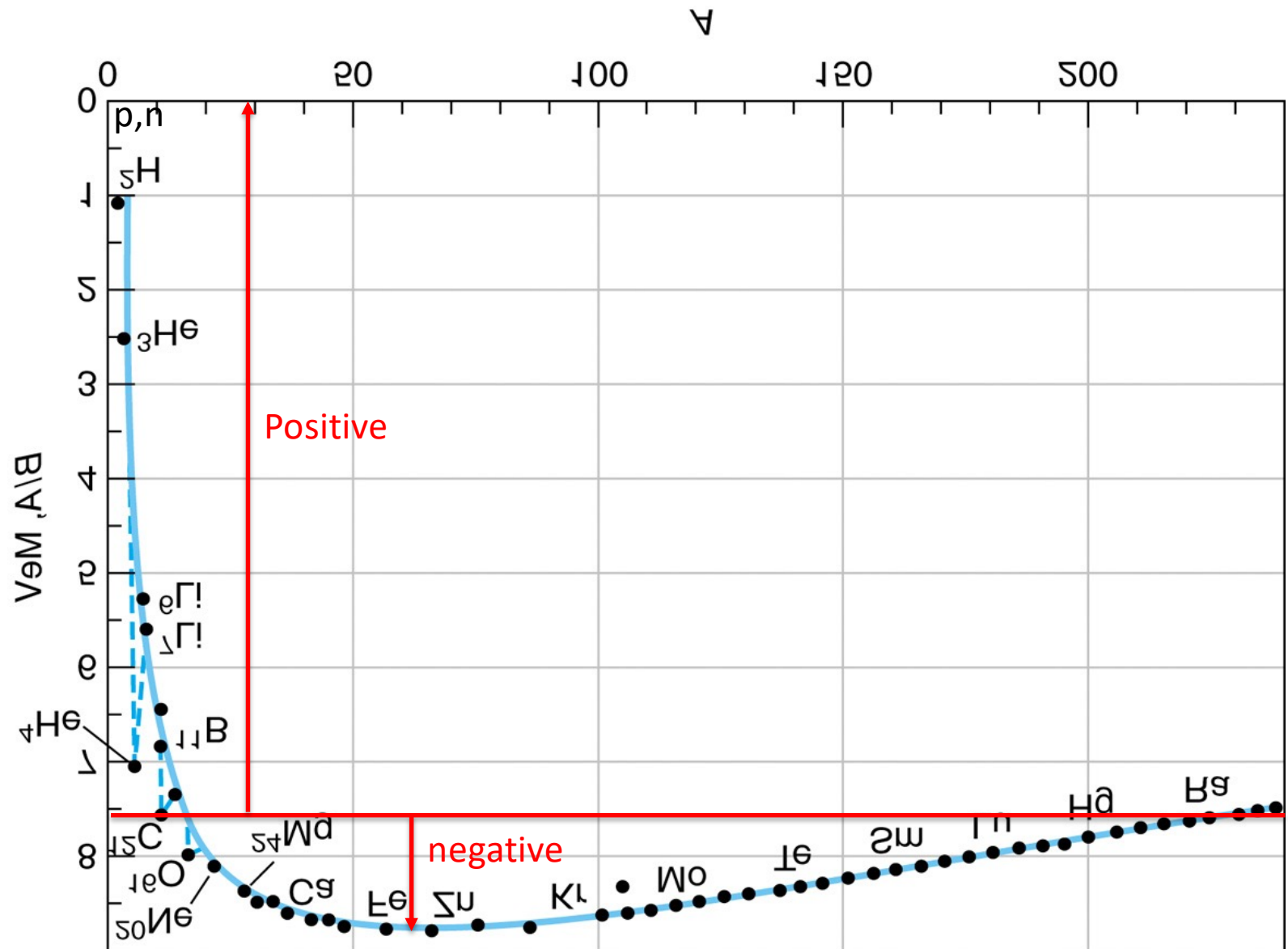
Central (saturation) density:

$$\rho_0 \approx 0.17 \text{ nucleons}/\text{fm}^3 = 3 \cdot 10^{17} \text{ kg}/\text{m}^3$$

Average density:  $0.13 \text{ nucleons}/\text{fm}^3$

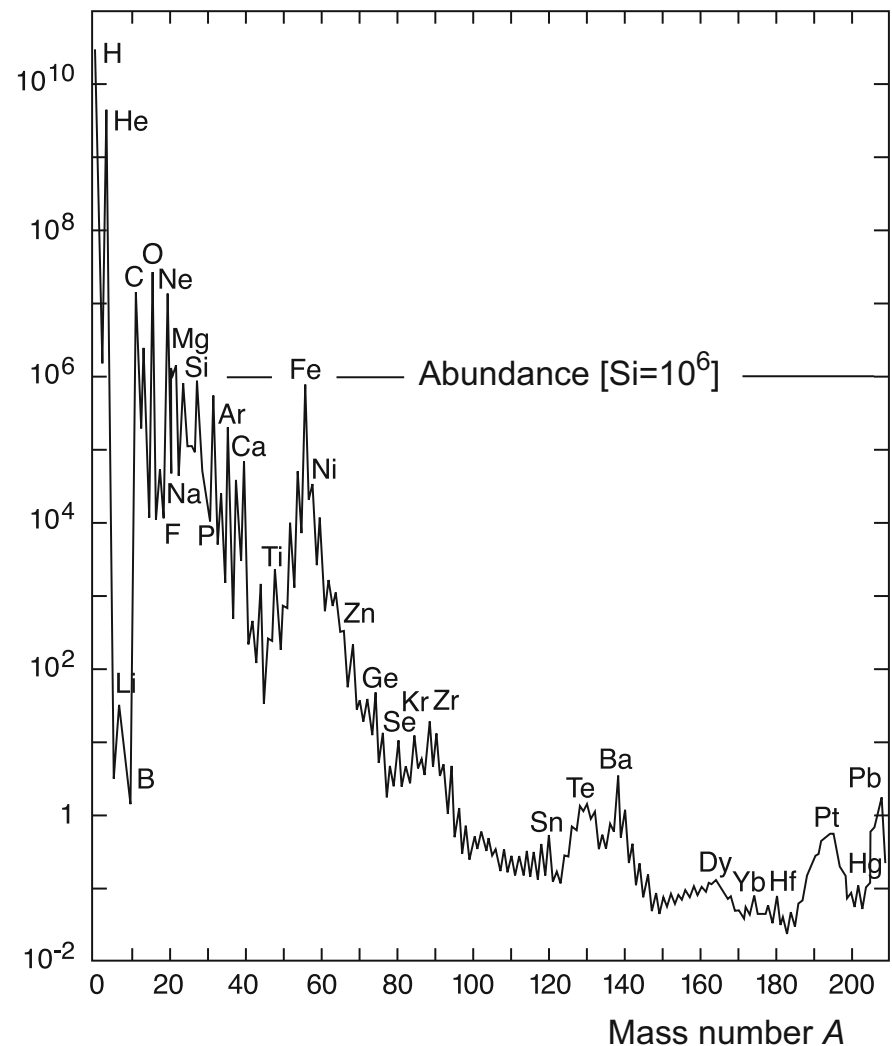


# Nuclear Mass excess per nucleon



# Partially explains abundance of elements

**Fig. 2.2** Abundance of the elements in the solar system as a function of their mass number  $A$ , normalised to the abundance of silicon ( $=10^6$ )



Full explanation requires:

- 1) INITIAL ("primordial") abundance (nearly all  $^1\text{H}$  and  $^4\text{He}$ )
- 2) Reaction path from these to heavier elements (stars and their collapse, supernovae, neutron star mergers,...)